

# Outline

- Relativistic Kinematics
  - ▶ (4-momentum)<sup>2</sup> invariance, invariant mass
  - ▶ Hypothesis testing, production thresholds
  - ▶ Cross-sections, flux and luminosity, accelerators
  - ▶ Particle lifetime, decay length, width
- Classification of particles
  - ▶ Fermions and bosons
  - ▶ Leptons, hadrons, quarks
  - ▶ Mesons, baryons
- Quark Model
  - ▶ Meson and baryon multiplets
  - ▶ Isospin, strangeness, c, ...
- Particle Interactions
  - ▶ Colour charge, QCD, gluons
  - ▶ Virtual particles and range of forces
  - ▶ Strong and weak decays, conservation rules
  - ▶ Parity, charge conjugation, CP
  - ▶ Weak decays of quarks
  - ▶ Charmonium and upsilon systems
- Electroweak Interactions
  - ▶ Charged and neutral currents
  - ▶ W, Z, LEP experiments
  - ▶ Higgs and the future
- LHC Experiments
- Future - introduction to accelerator physics

Today

- Lecture 9 (11 slides/page) - colour charge
  - Griffiths, pp. 181-188
  - Perkins (2nd edition), pp. 283-285

Previous lecture

- Lecture 8 (4 slides/page) - baryon wavefunction and colour charge
  - Griffiths, pp. 170-181
  - Perkins (2nd edition), pp. 150
  - Perkins (3rd edition), pp. 293-294

# Baryon wavefunction and colour

- Baryon wavefunction

$$\Psi_{\text{baryon}} = \Psi_{\text{spin}} \Psi_{\text{space}} \Psi_{\text{flavour}} \Psi_{\text{colour}}$$

has to be overall **antisymmetric** (Pauli Exclusion Principle) under interchange of any 2 quarks

- For J=3/2, uuu ( $\Delta^+$ ), ddd ( $\Delta^-$ ), sss ( $\Omega^-$ ) states exist

- ▶  $\Psi_{\text{spin}}$ ,  $\Psi_{\text{space}}$  and  $\Psi_{\text{flavour}}$  are all **symmetric**
- ▶ Therefore  $\Psi_{\text{colour}}$  has to be **antisymmetric**
- ▶ We extend this **assertion** to be true for **all baryons**

- Colour wavefunction for baryons (qqq) is always **antisymmetric** and is

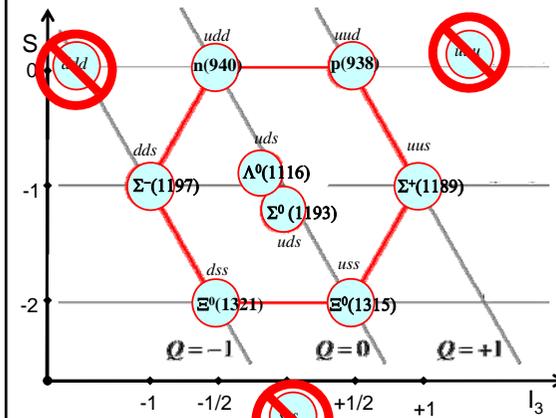
$$|rgb - grb + brg - rbg + gbr - bgr\rangle / \sqrt{6}$$

- ▶ This is the **colour singlet state** and **only this one** is allowed (of all 3<sup>3</sup> combinations)
- ▶ Subtle detail: identical particles are the quarks, **contrast with meson case**

# Baryon wavefunction and colour

- For J=1/2 baryon case,  $\Psi_{\text{space}}$  is still **symmetric**, so  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$  must also be **symmetric**
  - ▶ In J=1/2, states,  $|\uparrow\uparrow\downarrow\rangle$  etc., clearly symmetry is "mixed" – **neither fully symmetric or antisymmetric** – depending on which quarks are interchanged
  - ▶ To ensure overall **symmetric** behaviour of  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$ , need  $\Psi_{\text{flavour}}$  to have **complementary mixed symmetry** to  $\Psi_{\text{spin}}$
  - ▶ As  $\Psi_{\text{flavour}}$  is perfectly **symmetric** for uuu, ddd, sss states
  - ▶ ... and spin states such as  $|\uparrow\uparrow\downarrow\rangle$  are **mixed symmetry**,
  - ▶ ... **PEP excludes existence** of these combinations in J=1/2 states.
- This agrees with the observed baryon states
  - ▶ **Further evidence for colour quantum number**
  - ▶ In uud, etc. cases, there is one possibility for  $\Psi_{\text{flavour}}$  to **complement mixed symmetry spin wavefunction**
  - ▶ In uds case, two options for  $\Psi_{\text{flavour}}$  corresponding to  $\Lambda^0(1116)$  and  $\Sigma^0(1193)$
- Further details, see course web page references, esp. Griffiths pp. 187-188.

# J=1/2 Baryon Octet



[adapted from [http://en.wikipedia.org/wiki/File:Meson\\_nonet\\_-\\_spin\\_1.svg](http://en.wikipedia.org/wiki/File:Meson_nonet_-_spin_1.svg)]

