

## Outline

- Relativistic Kinematics
  - ▶ (4-momentum)<sup>2</sup> invariance, invariant mass
  - ▶ Hypothesis testing, production thresholds
  - ▶ Cross-sections, flux and luminosity, accelerators
  - ▶ Particle lifetime, decay length, width
- Classification of particles
  - ▶ Fermions and bosons
  - ▶ Leptons, hadrons, quarks
  - ▶ Mesons, baryons
- Quark Model
  - ▶ Meson and baryon multiplets
  - ▶ Isospin, strangeness, c, b, t quarks
- Particle Interactions
  - ▶ Colour charge, QCD, gluons
  - ▶ Virtual particles and range of forces
  - ▶ Strong and weak decays, conservation rules
  - ▶ Parity, charge conjugation, CP
  - ▶ Weak decays of quarks
  - ▶ Charmonium and epsilon systems
- Electroweak Interactions
  - ▶ Charged and neutral currents
  - ▶ W, Z, LEP experiments
  - ▶ Higgs and the future
- LHC Experiments
- Future - introduction to accelerator physics

Please see web page for specific references to textbooks and brief reviews from PDG.

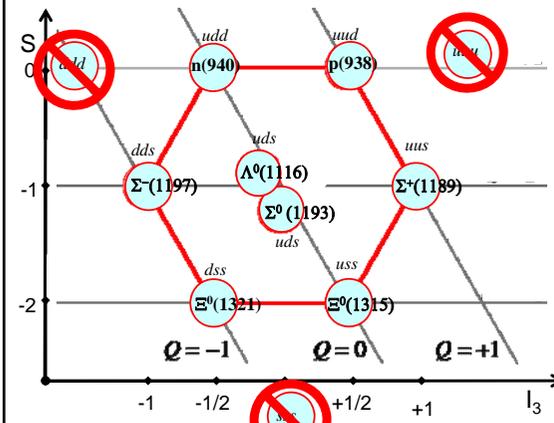
## Baryon wavefunction and colour

- Baryon wavefunction
  - $\Psi_{\text{baryon}} = \Psi_{\text{spin}} \Psi_{\text{space}} \Psi_{\text{flavour}} \Psi_{\text{colour}}$
- has to be overall **antisymmetric** (Pauli Exclusion Principle) under interchange of any 2 quarks
- Recall for J=3/2, uuu ( $\Delta^{++}$ ), ddd ( $\Delta^{-}$ ), sss ( $\Omega^{-}$ ) states,  $\Psi_{\text{colour}}$  has to be **antisymmetric** as  $\Psi_{\text{spin}}$ ,  $\Psi_{\text{space}}$  and  $\Psi_{\text{flavour}}$  are all **symmetric**
  - ▶ Important: we extend this **assertion** to be true for **all baryons**
- Colour wavefunction for baryons (qqq) is always **antisymmetric** and is
 
$$|rgb - grb + brg - rbg + gbr - bgr\rangle / \sqrt{6}$$
  - ▶ This is the **colour singlet state** and **only this one** is allowed (of all 3<sup>3</sup> combinations)
  - ▶ Subtle detail: identical particles are the quarks, **contrast with meson case**

## Baryon wavefunction and colour

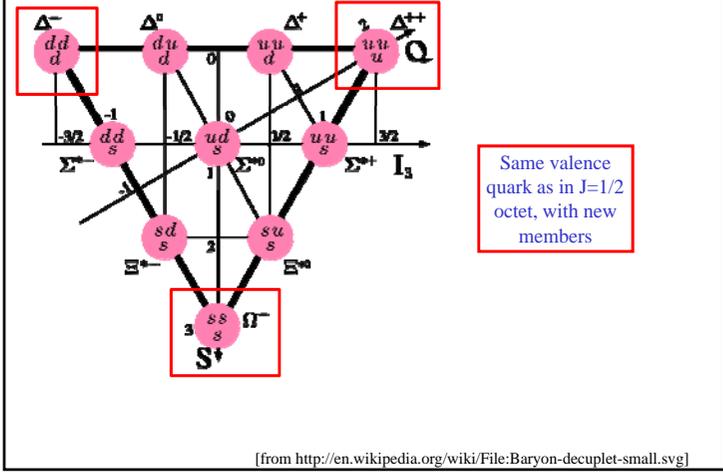
- For J=1/2 baryon case,  $\Psi_{\text{space}}$  is still symmetric, so  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$  must also be **symmetric**
  - ▶ In J=1/2, states,  $|\uparrow\downarrow\rangle$ , clearly symmetry is "mixed" – **neither fully symmetric or antisymmetric** – depending on which quarks are interchanged
  - ▶ To ensure overall symmetric behaviour of  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$ , need  $\Psi_{\text{flavour}}$  to have **complementary mixed symmetry** to  $\Psi_{\text{spin}}$
  - ▶ As  $\Psi_{\text{flavour}}$  is perfectly symmetric for uuu, ddd, sss states, **PEP excludes existence** of these combinations in J=1/2 states
- This agrees well with the observed baryon states
  - ▶ Further evidence for colour quantum number
- ▶ In uud, etc. cases, one possibility for  $\Psi_{\text{flavour}}$  to **complement mixed symmetry spin wavefunction**
- ▶ In uds case, two options for  $\Psi_{\text{flavour}}$  corresponding to  $\Lambda^0(1116)$  and  $\Sigma^0(1193)$
- Further details, see course web page references, esp. Griffiths pp. 187-188.

## J=1/2 Baryon Octet

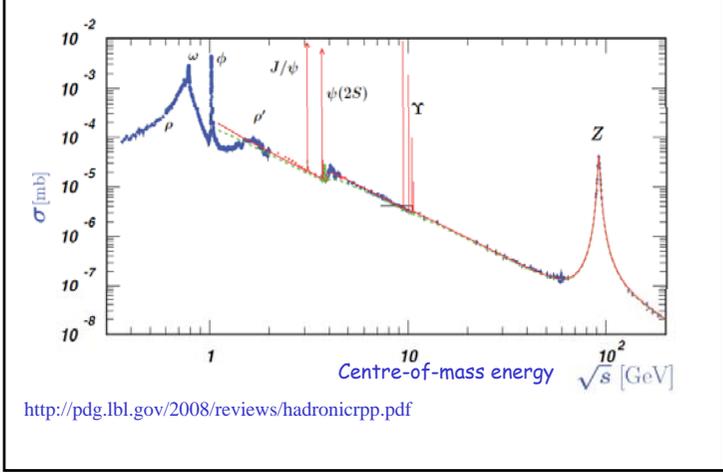


[adapted from [http://en.wikipedia.org/wiki/File:Meson\\_nonet\\_-\\_spin\\_1.svg](http://en.wikipedia.org/wiki/File:Meson_nonet_-_spin_1.svg)]

## J=3/2 Baryon Decuplet



## cross-section ( $e^+e^- \rightarrow \text{hadrons}$ )



## cross-section ratio: ( $e^+e^- \rightarrow \text{hadrons}$ ) / ( $e^+e^- \rightarrow \mu^+\mu^-$ )

