

# Outline

- Relativistic Kinematics
  - ▶ (4-momentum)<sup>2</sup> invariance, invariant mass
  - ▶ Hypothesis testing, production thresholds
  - ▶ Cross-sections, flux and luminosity, accelerators
  - ▶ Particle lifetime, decay length, width
- Classification of particles
  - ▶ Fermions and bosons
  - ▶ Leptons, hadrons, quarks
  - ▶ Mesons, baryons
- Quark Model
  - ▶ Meson and baryon multiplets
  - ▶ Isospin, strangeness, c, b, t quarks
- Particle Interactions
  - ▶ Colour charge, QCD, gluons
  - ▶ Virtual particles and range of forces
  - ▶ Strong and weak decays, conservation rules
  - ▶ Parity, charge conjugation, CP
  - ▶ Weak decays of quarks
  - ▶ Charmonium and upsilon systems
- Electroweak Interactions
  - ▶ Charged and neutral currents
  - ▶ W, Z, LEP experiments
  - ▶ Higgs and the future
- LHC Experiments
- Future - introduction to accelerator physics

Please see web page for specific references to textbooks and brief reviews from PDG.

# Baryon wavefunction and colour

## ■ Baryon wavefunction

- $\Psi_{\text{baryon}} = \Psi_{\text{spin}} \Psi_{\text{space}} \Psi_{\text{flavour}} \Psi_{\text{colour}}$

has to be overall **antisymmetric** (Pauli Exclusion Principle) under interchange of any 2 quarks

## ■ Recall for $J=3/2$ , $uuu$ ( $\Delta^{++}$ ), $ddd$ ( $\Delta^{-}$ ), $sss$ ( $\Omega^{-}$ ) states, $\Psi_{\text{colour}}$ has to be **antisymmetric** as $\Psi_{\text{spin}}$ , $\Psi_{\text{space}}$ and $\Psi_{\text{flavour}}$ are all **symmetric**

▶ Important: we extend this **assertion** to be true for **all baryons**

## ■ Colour wavefunction for baryons (qqq) is always **antisymmetric** and is

$$|rgb - grb + brg - rbg + gbr - bgr\rangle / \sqrt{6}$$

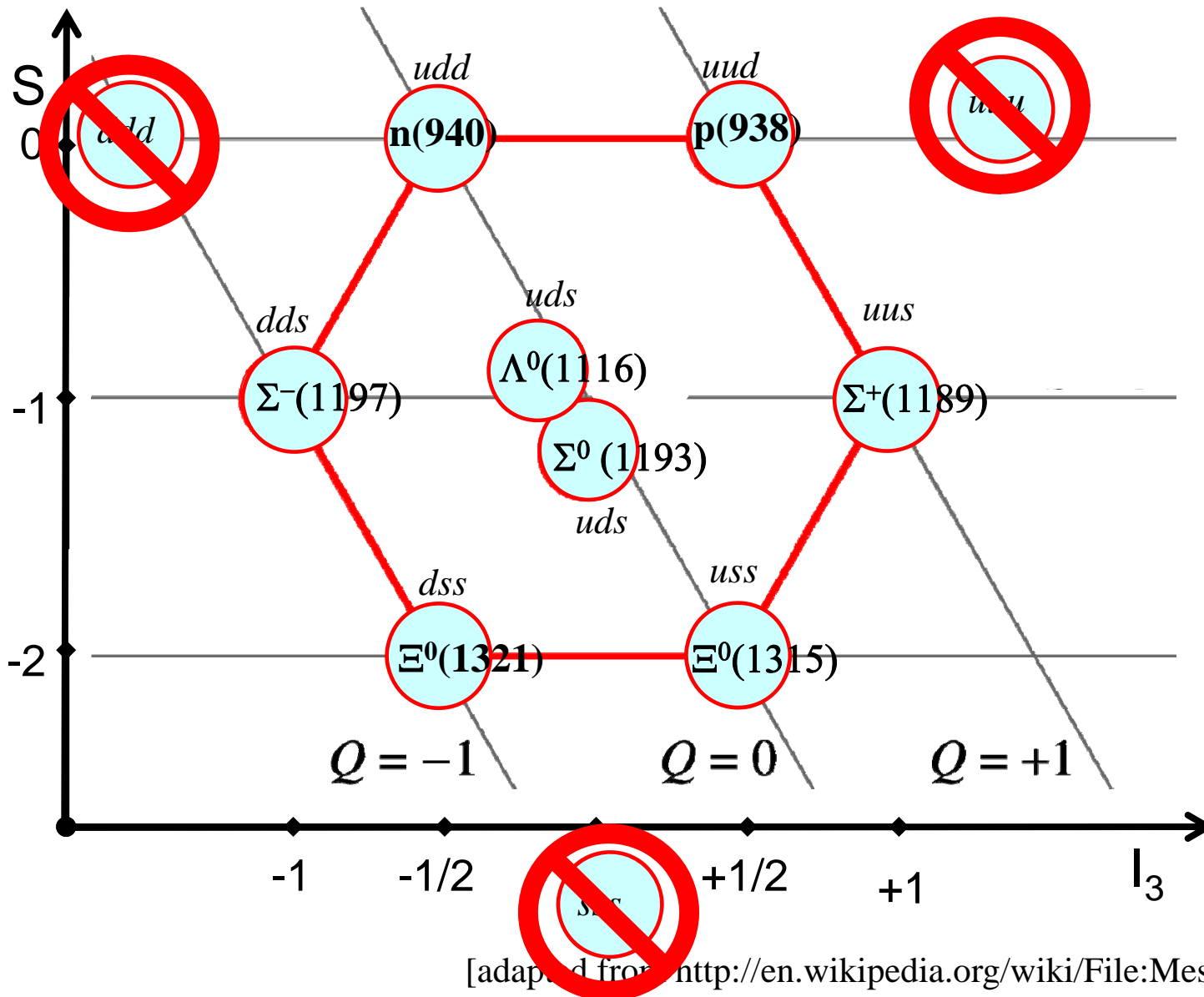
▶ This is the **colour singlet state** and **only** this one is allowed (of all  $3^3$  combinations)

▶ Subtle detail: identical particles are the quarks, **contrast with meson case**

# Baryon wavefunction and colour

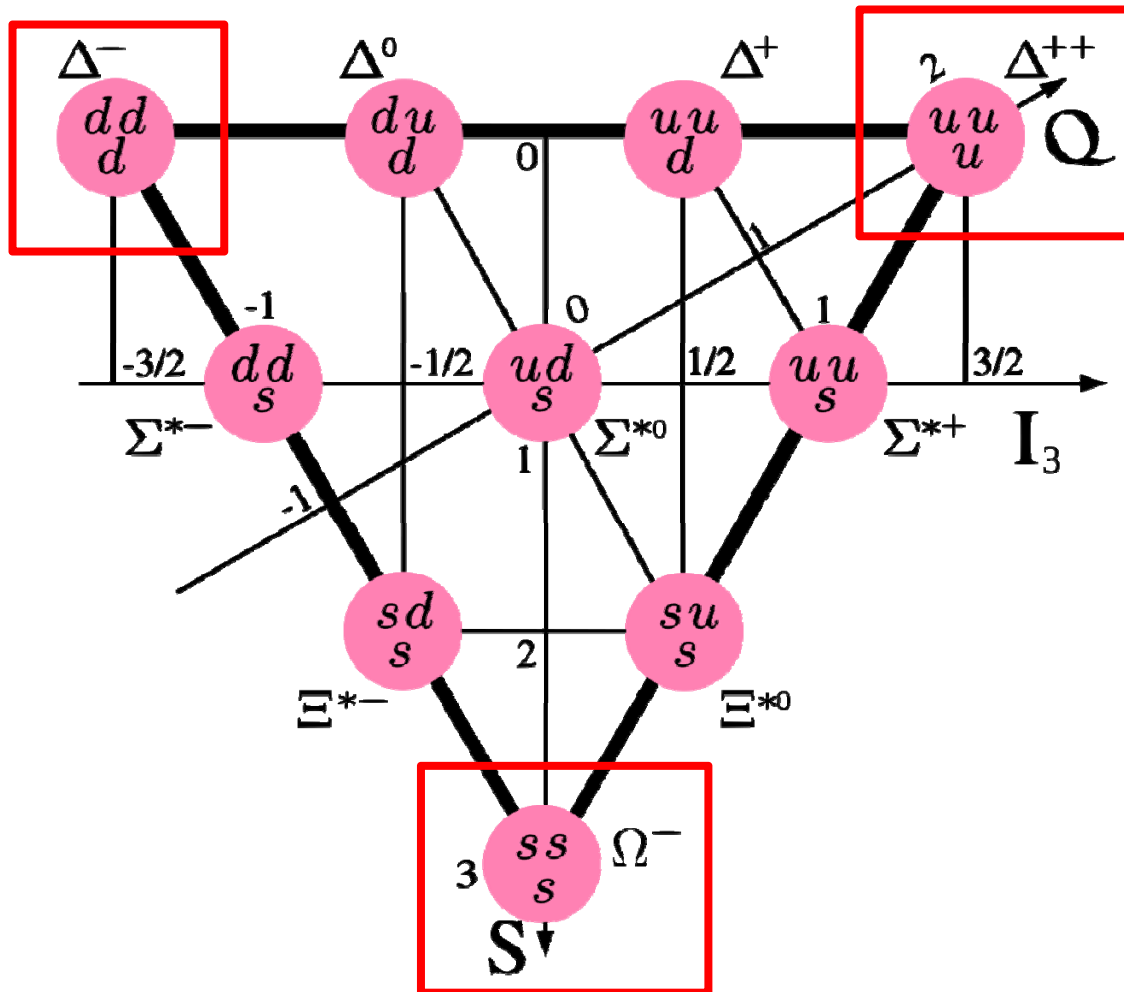
- For  $J=1/2$  baryon case,  $\Psi_{\text{space}}$  is still symmetric, so  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$  must also be **symmetric**
  - ▶ In  $J=1/2$ , states,  $|\uparrow\downarrow\downarrow\rangle$ , clearly symmetry is “mixed” – **neither** fully **symmetric** or **antisymmetric** – depending on which quarks are interchanged
  - ▶ To ensure overall symmetric behaviour of  $\Psi_{\text{spin}} \Psi_{\text{flavour}}$ , need  $\Psi_{\text{flavour}}$  to have **complementary mixed symmetry** to  $\Psi_{\text{spin}}$
  - ▶ As  $\Psi_{\text{flavour}}$  is perfectly symmetric for  $uuu$ ,  $ddd$ ,  $sss$  states, **PEP excludes existence** of these combinations in  $J=1/2$  states
- This agrees well with the observed baryon states
  - ▶ Further evidence for colour quantum number
  - ▶ In  $uud$ , etc. cases, one possibility for  $\Psi_{\text{flavour}}$  to **complement mixed symmetry spin wavefunction**
  - ▶ In  $uds$  case, two options for  $\Psi_{\text{flavour}}$  corresponding to  $\Lambda^0(1116)$  and  $\Sigma^0(1193)$
- Further details, see course web page references, esp. Griffiths pp. 187-188.

# J=1/2 Baryon Octet

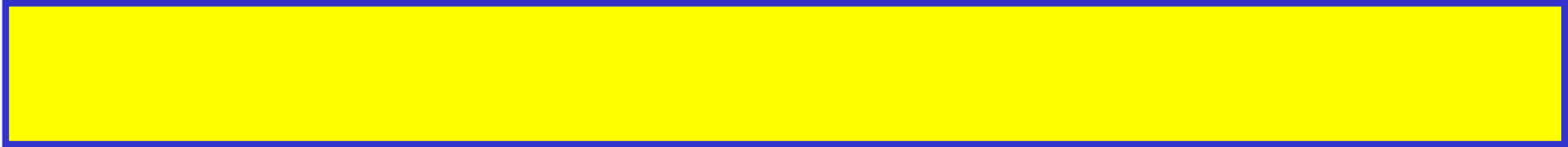


[adapted from [http://en.wikipedia.org/wiki/File:Meson\\_nonet\\_-\\_spin\\_1.svg](http://en.wikipedia.org/wiki/File:Meson_nonet_-_spin_1.svg)]

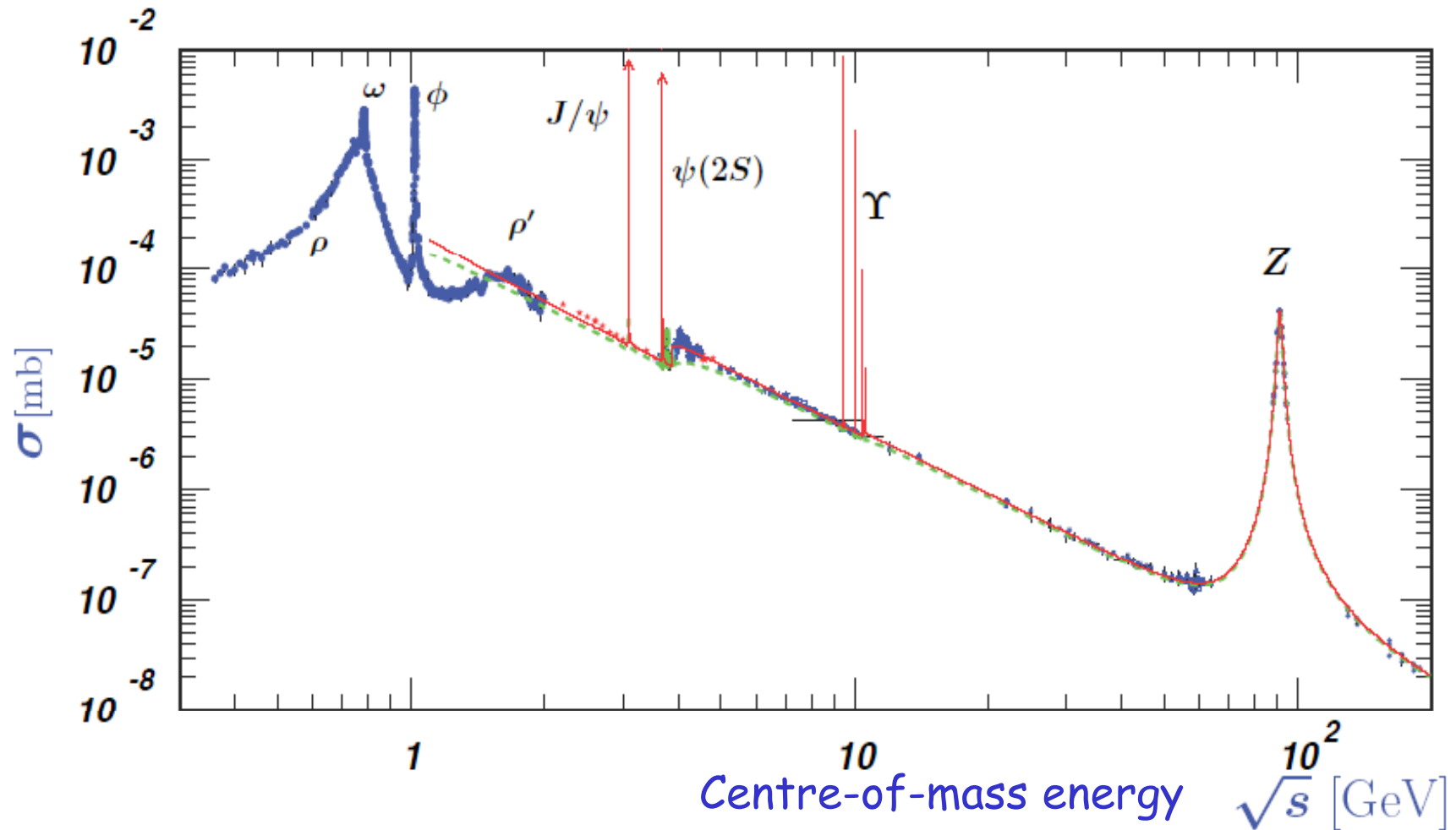
# J=3/2 Baryon Decuplet



Same valence quark as in J=1/2 octet, with new members

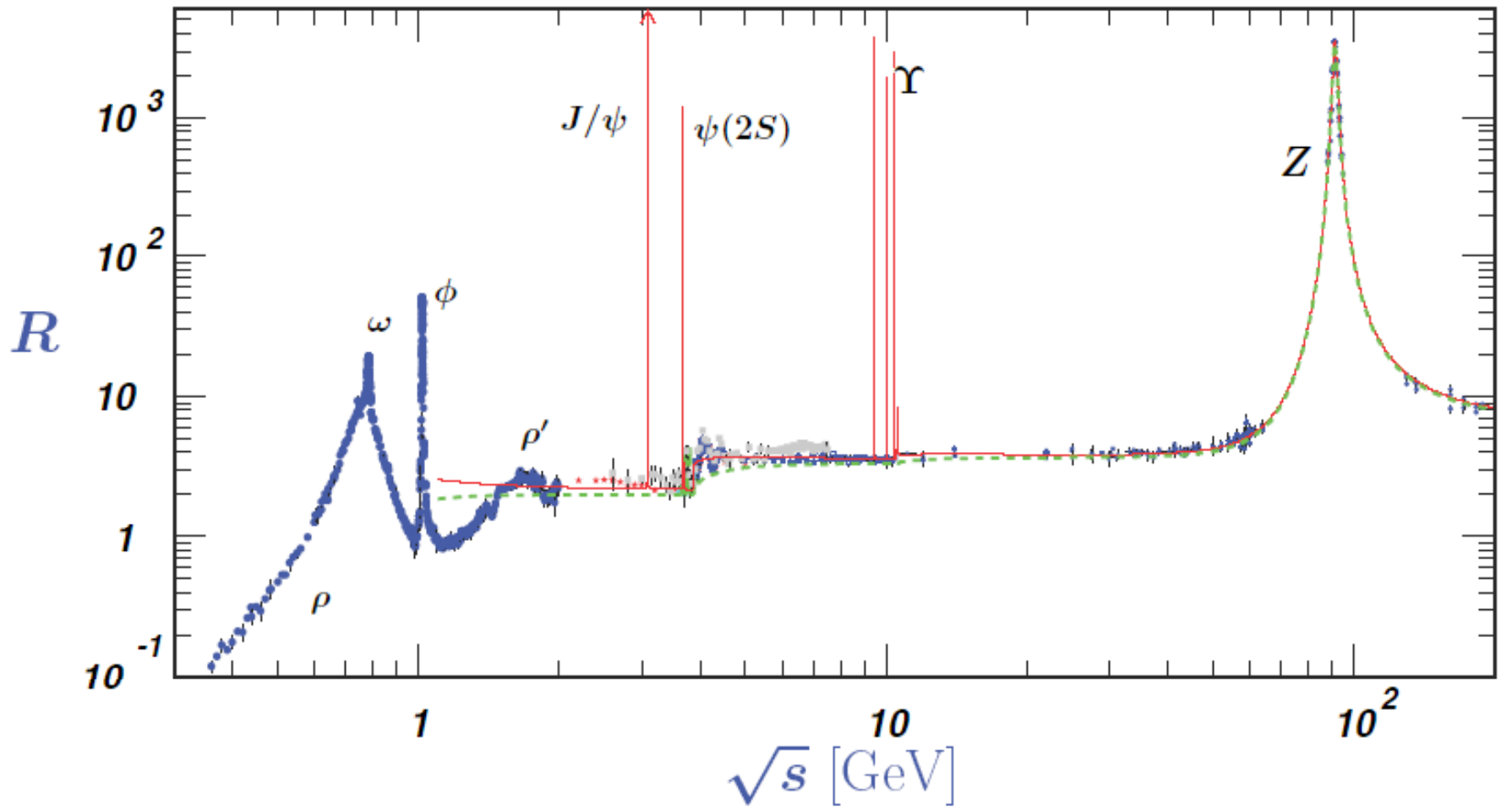


# cross-section ( $e^+e^- \rightarrow \text{hadrons}$ )



<http://pdg.lbl.gov/2008/reviews/hadronicrpp.pdf>

**cross-section ratio:  $(e^+e^- \rightarrow \text{hadrons}) / (e^+e^- \rightarrow \mu^+\mu^-)$**



<http://pdg.lbl.gov/2008/reviews/hadronicrpp.pdf>