

# Outline

- Relativistic Kinematics
  - ▶ (4-momentum)<sup>2</sup> invariance, invariant mass
  - ▶ Hypothesis testing, production thresholds
  - ▶ Cross-sections, flux and luminosity, accelerators
  - ▶ Particle lifetime, decay length, width
- Classification of particles
  - ▶ Fermions and bosons
  - ▶ Leptons, hadrons, quarks
  - ▶ Mesons, baryons
- Quark Model
  - ▶ Meson and baryon multiplets
  - ▶ Isospin, strangeness, c, b, t quarks
- Particle Interactions
  - ▶ Colour charge, QCD, gluons, fragmentation, running couplings
  - ▶ Strong and weak decays, conservation rules
  - ▶ Virtual particles and range of forces
  - ▶ Parity, charge conjugation, CP
  - ▶ Weak decays of quarks
  - ▶ Charmonium and upsilon systems
- Electroweak Interactions
  - ▶ Charged and neutral currents
  - ▶ W, Z, LEP experiments
  - ▶ Higgs and the future
- LHC Experiments' Results
- ☺ Future - introduction to accelerator physics ☺

Today

- [Lecture 21 \(4 slides/page\)](#) - Z couplings, decay widths, couplings, Higgs
  - Martin and Shaw, pp. 225-229

Previous lecture

- [Lecture 20 \(4 slides/page\)](#) Weak neutral currents (Z) and experiments
  - Perkins, p317-318;
  - Griffiths, pp. 72-74;

# For $e^+e^-$ experiments

- **Vertex detector** - Usually Si-based, ~10um pixel or strip readout, measures displaced decay vertices (and improves momentum measurement)
- **Tracking chamber** - measures momentum from curvature in B field; ionisation of gas and (in drift chamber) readout on sense wires or (in TPC) end plates. The most recent designs for future accelerators consider using Si detectors.
- **Magnetic field (solenoid)** - provides bending of charged particle trajectories in plane perpendicular to beam axis. (May be located in front or after calorimeters.)
- **EM calorimeter** - sampling or homogeneous, measures: full energy of electrons, photons; fraction for charged hadrons; minimal amount for muons

# For $e^+e^-$ experiments

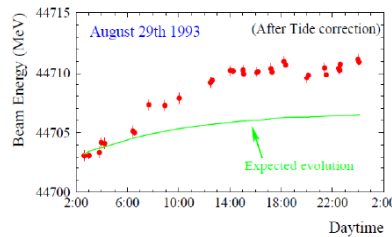
- **Hadronic calorimeter** - sampling, measures energy of hadrons (especially neutral hadrons).
- **Muon detectors** - outermost detector, any particle that passes through all previous material is assumed to be a muon (almost all others stopped in hcal or previous).
- **Luminosity detectors** - e.m. calorimeters located at very small angles to beam axis (~40 mrad), detect high energy  $e^+e^-$  from Bhabha scattering process, comparison with theoretical cross-section for which gives luminosity at the experiment
- At LEP, there were 4 detectors: Aleph, Opal ("General Purpose Detectors" using established technology); Delphi ("General purpose detector" with emphasis on new technology); L3 (emphasis on muonic final states, very small main tracking system)

# Z boson mass determination

- Achieved relative precision of  $\sim 10^{-5}$  on Z boson mass,  $m_Z$
- Not possible by "direct reconstruction" of kinematics of observed particles (experimental resolutions)
- Achieved by
  - ▶ Observing very large number of events ( $Z^0$  resonance enhances cross-section by  $\sim 5000$  for  $E_{cm} \sim m_Z$ )
  - ▶ Classifying final states
  - ▶ Using " $N=L\sigma$ " to determine cross-section
  - ▶ Comparing measured cross-section with *very accurate theoretical description* of  $\sigma(e^+e^- \rightarrow ff)$  as  $f(m_Z, \Gamma_Z, E_{cm}, \dots)$ 
    - ⇒ Requires many higher order diagrams to be calculated
- Experimental determination of centre-of-mass energy ("LEP beam energy", lecture 20) a particularly hard measurement, emphasis on systematic uncertainties...

# LEP beam energy measurement I

- Precise beam energy by "resonant depolarisation" measurements
  - A single beam of polarised  $e^-$  is stored in the LEP accelerator and the measured precession frequency of  $e^-$  spins allows  $E_{\text{beam}}$  to be measured to a precision of  $<1$  MeV (at  $E_{\text{beam}} \sim 45$  GeV)
  - However, this cannot be used during recording  $e^+e^-$  collisions, and therefore requires dedicated running of the accelerator.
  - This is only performed infrequently, because the time taken out for these measurements is time not available to collect Z decay events (reducing statistical precision of the cross-section measurements themselves).
  - Found to be  $\sim 10$  MeV variation between these resonant depolarisation runs...



# Systematics on LEP $E_{\text{beam}}$ measurement I

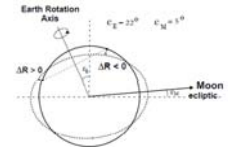
## Earth tides

- Movement of moon/sun - Earth cause tides, which raise and lower the Earth crust (as well as the oceans)
- Variation at Geneva  $\sim 25$ cm vertical motion per day, inducing change in circumferences of LEP by  $\sim \pm 0.5$ mm.
- Although a small effect relative to the 27km circumference, this changes  $E_{\text{beam}}$  because the  $e^-$  rotational frequency in the accelerator is fixed by the radio-frequency acceleration system and therefore induces a small offset from the centre of the quadrupole (focussing) magnets.
- This changes  $E_{\text{beam}}$  in the centre of each experiment
- The effect was predicted in advance, calculated, verified and taken into account by the experiments ☺

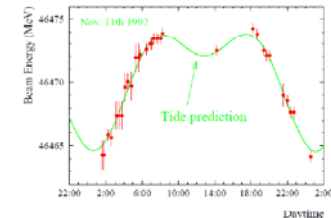
Tide bulge of a celestial body of mass  $M$  at a distance  $d$ :

$$\Delta R \sim \frac{M}{2d^3}(3\cos^2\theta - 1)$$

$\theta$  = angle(vertical, the celestial body)



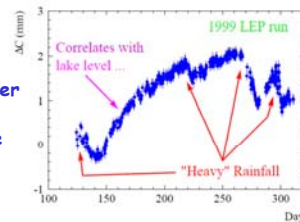
Fall of 1992 : The historic tide experiment !



# Systematics on LEP $E_{\text{beam}}$ measurement II

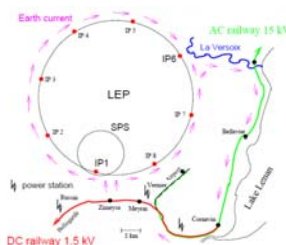
## Water level

- Level of water in Lac Lemman also affects the LEP circumference due to strain.
- The energy was observed to be correlated with the water level in the lake
- However, this is not as easy to calculate reliably (unlike earth tides) and so a small residual uncertainty was assigned due to this source.



## Leakage from French trains (TGV)

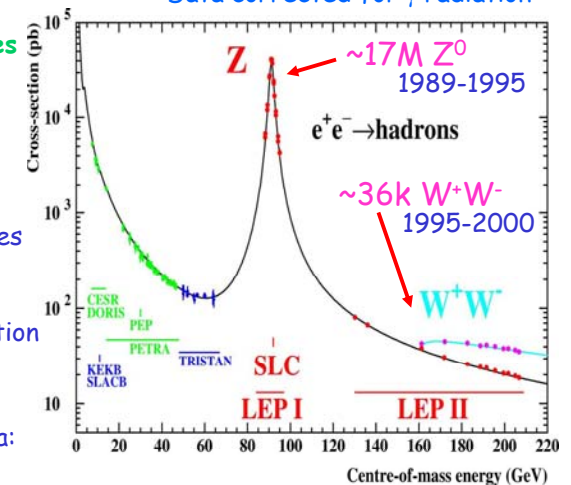
- Relatively large uncertainties were still observed in  $E_{\text{beam}}$  over each day and not understood for years.
- The effect was finally correlated to the TGV timetable and stray leakage currents to pass along the (metal) LEP beam pipe.
- The effects were found to be absent during a measurement that took place by chance when there was an industrial strike which halted TGV operation.
  - The French electric trains are supplied by a DC current, some leaks to ground and completes a circuit by the path of least electrical resistance, causing different electrical currents in different sectors of the LEP accelerator, and these currents were found to be very highly correlated with the measured beam energy. This was the final source of uncertainty to be discovered!



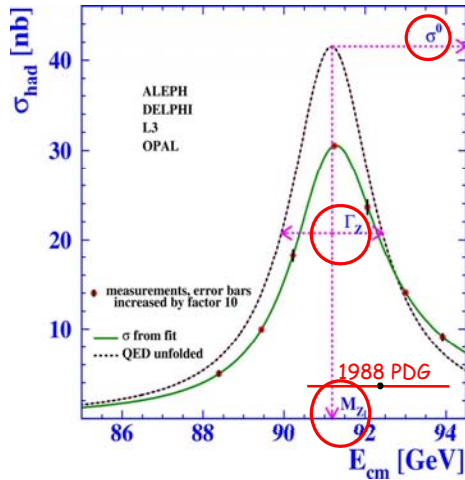
# LEP: 1989-2001

- Precise measurements  $\sqrt{s} \sim m_Z$ 
  - No. neutrinos
  - Couplings, mixing angles
- $f\bar{f}$  physics above  $m_Z$
- $W^+W^-$  production, properties
- Neutral boson pair production
- SM interpretations of data:
  - Higgs mass

Data corrected for  $\gamma$  radiation



# LEP Lineshape: 1989+...final results



- 3 parameters:  $m_Z, \Gamma_Z, \sigma_{had}^0$
- Observe  $e^- \rightarrow e^- \gamma \rightarrow f \bar{f}$  via  $Z/\gamma$
- ...EW radiative corrections absorbed in effective couplings
- Deconvolve to Born cross-section

Obtain

$$m_Z = 91,187.5 \pm 2.1 \text{ MeV}$$

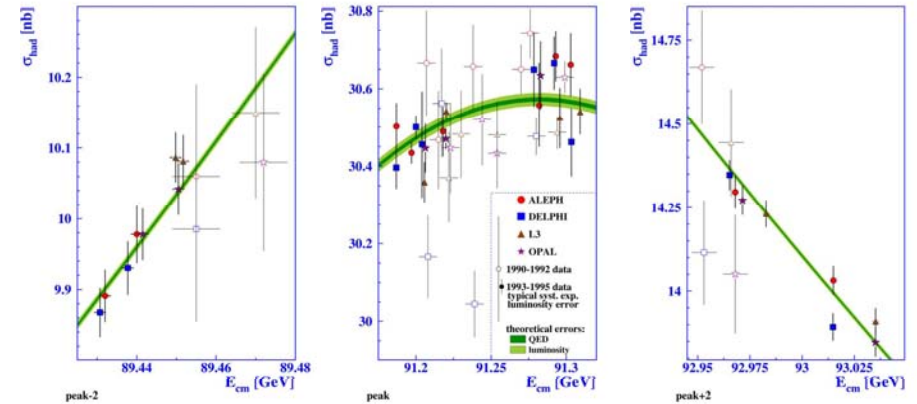
$$\Gamma_Z = 2,495.2 \pm 2.3 \text{ MeV}$$

$$\sigma_{had}^0 = 41.540 \pm 0.037 \text{ nb}$$

Combined measurements, LepI sample

Final LEPI "Z<sup>0</sup> lineshape" measurements  
See Physics Reports, Vol. 427, Nos. 5-6, May 2006

# Fine details of LepI Cross-Section Data



All 4 LEP experiments and years of "Lep I" ( $E_{cm} \sim m_Z$ )  
Mass of Z<sup>0</sup> from cross-section measurement ("counting experiment")  
Contrast with mass of W from measured energy and momenta ("direct reconstruction")

# No. of Neutrino Generations

- "Invisible width",  $\Gamma_{inv} = \Gamma_Z - \Gamma_{had} - 3 \Gamma_\ell$
- No. of generations =  $\Gamma_{inv} / \Gamma_\nu^{SM}$  SM:  $\Gamma_\nu^{SM} = \frac{G_F m_Z^3}{6\pi\sqrt{2}} (c_v^2 + c_a^2) \approx 166 \text{ MeV}$   
► Measure  $\Gamma_{inv}$
- $c_v + c_a$  are vector and axial vector couplings of neutrino to Z
- Direct: measure  $\sigma(e^+e^- \rightarrow \nu\bar{\nu}\gamma)$  soft  $\gamma$  + nothing else...challenging!
- Indirect: measure  $m_Z, \Gamma_Z, R_\ell, \sigma_{had}^0$

$$\Gamma_{inv} / \Gamma_\nu^{SM} = \left( \frac{12\pi}{m_Z^2 \sigma_{had}^0} \right)^{\frac{1}{2}} - R_\ell - 3$$

$$\sigma_{had}^0 \equiv \frac{12\pi\Gamma_e\Gamma_{had}}{(m_Z\Gamma_Z)^2}$$

⇒  $N_\nu = 2.9841 \pm 0.0083$  for  $m_\nu \leq \frac{1}{2}m_Z \sim 45 \text{ GeV}$

- For  $N_\nu = 3$ , width from new Z decay modes =  $-2.7 \pm 1.6 \text{ MeV}$
- Still room for heavy or sterile neutrinos

# P and T transformations

Observable	Parity transform
Position, $r$	$-r$ (vector)
Momentum, $p$	$-p$ (vector)
Spin, $\sigma$	$\sigma$ (axial vector)
Longitudinal polarisation, $\sigma \cdot p$	$-\sigma \cdot p$ (pseudoscalar)
Electric field, $E$	$-E$ (vector)
Magnetic field, $B$	$B$ (axial vector)
Magnetic dipole moment, $\sigma \cdot B$	$\sigma \cdot B$ (scalar)
Electric dipole moment, $\sigma \cdot E$	$-\sigma \cdot E$ (pseudoscalar)

# Z couplings to fermions

fermion	$c_v$	$c_a$
$\nu_e, \nu_\mu, \nu_\tau$	$\frac{1}{2}$	$\frac{1}{2}$
$e^-, \mu^-, \tau^-$	$-\frac{1}{2} + 2\sin^2\theta_W$	$-\frac{1}{2}$
$u, c, t$	$\frac{1}{2} - (4/3)\sin^2\theta_W$	$\frac{1}{2}$
$d, s, b$	$-\frac{1}{2} + (2/3)\sin^2\theta_W$	$-\frac{1}{2}$

$$c_v/c_a = 1 - 4Q_f \sin^2\theta_W$$

where  $Q_f$  is fermion e.m. charge (units of  $|e|$ ), for all fermion species

$\theta_W$  is the "weak mixing angle" (determined experimentally)

Connects weak and e.m. charges by  $e = g \sin\theta_W$

Measured value  $\sin^2\theta_W = 0.232$

At "lowest order",  $M_w = M_Z \cos\theta_W$

# e.g. SM Combined Fits to Data

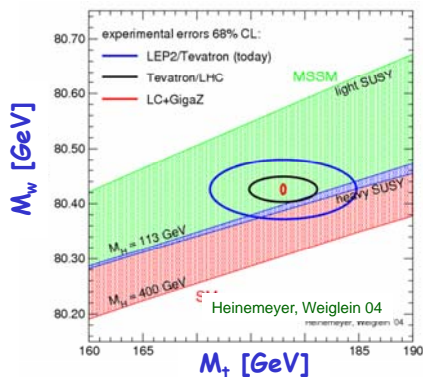


Consistency of data with SM, illustrated by "pull" values i.e. for each observable,  $o_i$ ,  $|o_i - SM \text{ fit}_i| / \text{error}(o_i)$

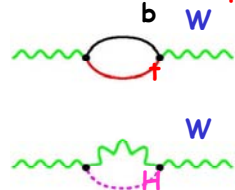
See [LEP Electroweak Working Group](http://lepewwg.web.cern.ch/LEPEWWG/)

<http://lepewwg.web.cern.ch/LEPEWWG/>

# Precise measurements consistency and predictions



$M_w$  sensitive to top, Higgs via loops



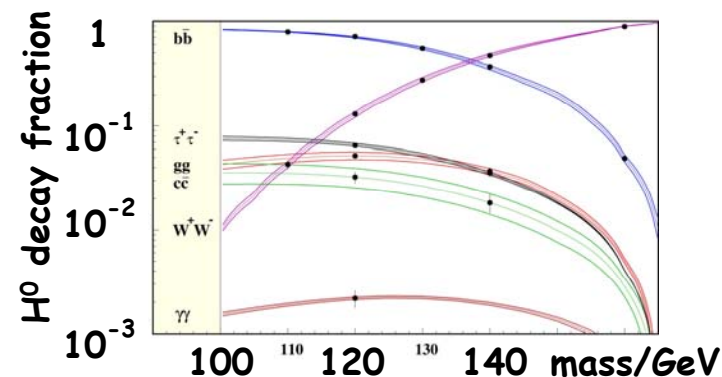
[Heinemeyer et al (LHCLC report)]

	$\delta m_w$ (MeV)	$\delta m_{top}$ (GeV)	$\delta \sin^2\theta_{eff} \times 10$
In 2004	34	3.9	17
TeV Run 2	16	1.4	29
LHC	15	1.0	14-20
ILC-GigaZ	7	0.1	1.3

[after Stirling, ECFA w/s, Durham Sep.04]

# Higgs in $e^+e^-$ collisions

Multi-jets: Higgs spectroscopy, WW/ZZ,  $\tau\tau$  decays



No ambiguity in predictions

Very precise measurement only possible at lepton colliders

