

Outline

- Relativistic Kinematics
 - ▶ (4-momentum)² invariance, invariant mass
 - ▶ Hypothesis testing, production thresholds
 - ▶ Cross-sections, flux and luminosity, accelerators
 - ▶ Particle lifetime, decay length, width
- Classification of particles
 - ▶ Fermions and bosons
 - ▶ Leptons, hadrons, quarks
 - ▶ Mesons, baryons
- Quark Model
 - ▶ Meson and baryon multiplet
 - ▶ Isospin, strangeness, c, b, t quarks
- Particle Interactions
 - ▶ Colour charge, QCD, gluons
 - ▶ Virtual particles and range of forces
 - ▶ Strong and weak decays, conservation rules
 - ▶ Parity, charge conjugation, CP
 - ▶ Weak decays of quarks
 - ▶ Charmonium and epsilon systems
- Electroweak Interactions
 - ▶ Charged and neutral currents
 - ▶ W, Z, LEP experiments
 - ▶ Higgs and the future
- LHC Experiments
- Future - introduction to accelerator physics

Today

- Lecture 10 (4 slides/page) - QCD
 - Griffiths, pp. 66-72, 173, 283-301
 - Perkins, pp. 291-293, 303, 307
 - Williams, pp. 179-181
 - PDG review of QCD - earlier parts too detailed, suggest starting at Sect. 9.3

Previous lecture

- Lecture 9 (4 slides/page) - colour charge
 - Griffiths, pp. 181-188
 - Perkins, pp. 283-285

Quantum Field Theories in PP - QED and QCD

- QED developed ~1948 by Feynman, Tomonaga, Schwinger
- Locally Gauge Invariant Theory
 - ▶ Effectively equivalent to having an arbitrary zero of electric potential
 - ▶ Conservation of charge leads to "choice of gauge" (in Maxwell Equations)
 - ▶ Symmetry of the theory (physics of interactions the same after any global change in potential)
 - ⇒ leads to charge conservation (Noether's Theorem)
- The "local" aspect extends idea to arbitrary choice at any point in space
- QED, gauge symmetry group is called U(1)
- QCD, gauge symmetry group is called SU(3) - three colour charges
 - ▶ "non-Abelian" theory (order of operations such as rotations important in 3d)
- Renormalizable Theory
 - ▶ Can be used for real calculations in perturbation theory without introducing uncontrolled divergences (infinities)
- Concepts advanced, will not do any more than skim surface (apologies!)
 - ▶ Interested in details, will put further references on web

Quantum ElectroDynamics - QED

- Measured/predicted to ~6 parts in 10¹⁰ precision
- D. Hanneke, S. Fogwell and G. Gabrielse, Phys. Rev. Lett. 100, 120801 (2008).

Examples of what is involved in calculations to reach such precision...

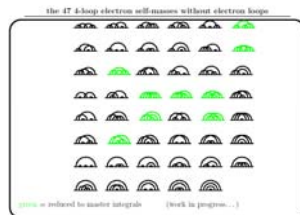
Example of numerical value of a Master Integral

$$M_{\text{fin}} = \frac{5}{2^3} - \frac{45}{2^3} + \frac{420}{2^3} - \frac{19637}{1728} - 141.7221561966470904996791$$

$$- 521.18545696929141175196 - 3447.99362972986117613115^2$$

$$- 17941.271771499964931007922^3 - 101732.616333171212129569366^4 - \dots$$

$$= \frac{4-D}{2}$$



Contribution of a 4-loop quadruple-cross diagram

$$= (2329 \text{ integrals}) = \sum_{j=1}^{10} \frac{P_j(D)}{Q_j(D)} M_j(D) \quad 140 \text{ Master Integrals}$$

M_1 M.I. with 11 denominators

$$P_1(D) = \text{polynomial of degree 11}$$

$$Q_1(D) = 5(D-1)(D+2)(D-3)(3D-16)(5D-19)(5D-22)$$

M_{10} M.I. with 4 denominators (factorize into 4 1-loop tadpoles)

$$P_{10}(D) = \text{polynomial of degree 56}$$

$$Q_{10}(D) = 3(58899(D-4)(D+2)(D-1)^2(D-3)^2(D-4)^3$$

$$(D-5)^2(D-6)(D-8)(2D-5)^2(D-7)^2(2D-9)^2(2D-11)$$

$$(2D-13)(3D-8)^2(3D-10)^2(3D-11)^2(3D-13)(4D-11)$$

$$(5D-12)(5D-13)(5D-14)(5D-16)(5D-17)(5D-18)$$

$$(5D-19)(5D-21)(5D-22)(7D-16)(30D^2-50D+86)$$

Strong Coupling "constant", α_s

- α_s the fundamental, universal QCD parameter
- Standard Model predicts "momentum scale", Q (~ \sqrt{s}) evolution, but not the absolute value of α_s
 - ▶ Perturbative effects, varying as $\sim 1/\ln Q$
 - ▶ Non-perturbative effects, varying as $\sim 1/Q$
- Test: measure different processes, energies
- Intuitive techniques in e^+e^-
- Precision low, $\theta(\%)$ cf. electroweak $\theta(10^{-5})$

