















No. of Neutrino Generations
■ "Invisible width", $\Gamma_{inv} = \Gamma_Z - \Gamma_{had} - 3 \Gamma_\ell$ ■ No. of generations = $\Gamma_{inv} / \Gamma_v^{SM}$ SM: $\Gamma_v^{SM} = \frac{G_F m_Z^3}{6\pi\sqrt{2}} (g_{v,v}^2 + g_{a,v}^2) \approx 166 \text{ MeV}$ → Measure Γ_{inv}
Direct: measure $\sigma(e^+e^- \rightarrow v\bar{v}\gamma)$ soft γ + nothing elsechallenging!
■ Indirect: measure m_Z , Γ_Z , R_ℓ , σ_{had}° $\sigma_{had}^\circ \equiv \frac{12\pi\Gamma_e\Gamma_{had}}{(m_Z\Gamma_Z)^2}$
$\Gamma_{\rm inv} / \Gamma_{\rm v}^{\rm SM} = \left(\frac{12\pi}{m_Z^2 \sigma_{\rm had}^2}\right)^{\frac{1}{2}} - R_{\ell} - 3$
$\Rightarrow \ \ N_v = 2.9841 \pm 0.0083 \ \ \text{for } m_v \le \frac{1}{2} m_Z \sim 45 \ \text{GeV}$
 For N_v = 3, width from new Z decay modes = -2.7 ± 1.6 MeV Still room for heavy or sterile neutrinos