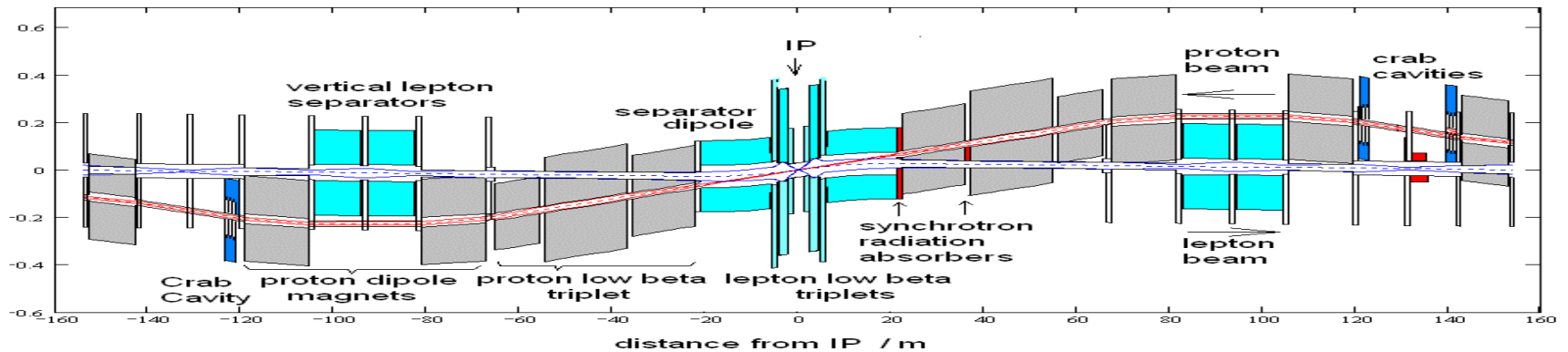


Study of the Luminosity of LHeC, a Lepton Proton Collider in the LHC Tunnel

CERN June 14 2006
F. Willeke, DESY



LHeC Design Goals

Luminosity $L = 1 \cdot 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

Energy $E_{\text{cm}} = 1.4 \text{ TeV}$

These input parameters are subject to be altered by further iterations

But this study assumes these parameters to be fixed

Design Assumptions

based on LHC Proton beam parameters

Energy	$E_p = 7 \text{ TeV}$
Particles per Bunch	$N_p = 1.68 \cdot 10^{11}$
Emittance	$\varepsilon_{Np} = 3.75 \text{ rad}\mu\text{m}$
Bunch spacing	$\tau_b = 25 \text{ ns}$
Bunch Length	$\sigma_p = 7.55 \text{ cm}$



$$E_e = 70 \text{ GeV}$$

Circumference = 26658.883 m

Luminosity

$$L = \frac{N_p \cdot N_e \cdot f_{rev} \cdot n_b}{2 \cdot \pi \cdot \sqrt{\varepsilon_{xp} \beta_{xp} + \varepsilon_{xe} \beta_{xe}} \cdot \sqrt{\varepsilon_{yp} \beta_{yp} + \varepsilon_{ye} \beta_{ye}}}$$

Matched beam cross sections at IP $\sigma_{xp} = \sigma_{xe}, \quad \sigma_{yp} = \sigma_{ye}$

Lepton Beam-beam tune shift limit to be avoided

$$L = \frac{I_e \cdot N_p \cdot \gamma_p}{2\pi \cdot e \cdot \varepsilon_{Np} \cdot \sqrt{\beta_{xp} \cdot \beta_{yp}}}$$

With the proton beam brightness given by LHC, $N_p \gamma_p / \varepsilon_{Np} = 3.2 \cdot 10^{20} \text{m}^{-1}$



$$\frac{I_e}{\sqrt{\beta_{xp} \beta_{yp}}} = 0.063 \frac{\text{A}}{\text{m}}$$

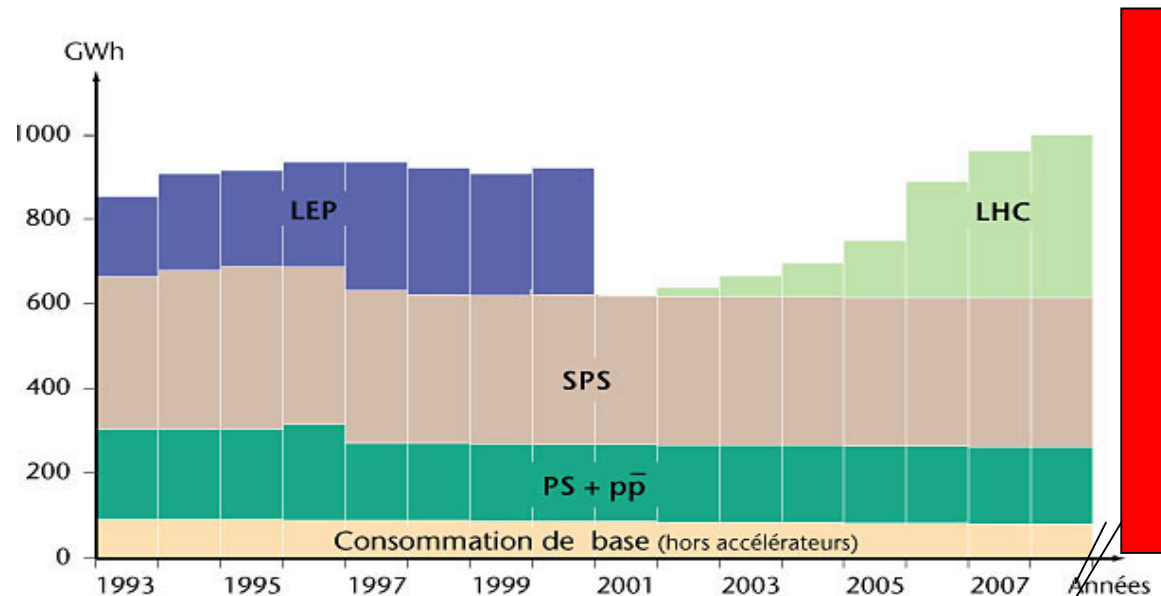
Lepton Beam Current

Assumptions: Limited by RF Power only
depends on Bending radius

$$\rho = 80\% \cdot (C_{\text{LHC}} - 8 \cdot L_{\text{straight}}) / 2\pi = 2886 \text{ m}$$

$$eU_{\text{loss}} = C_g E_e^4 / (e\rho) = 734 \text{ MeV}$$

CERN Power Consumption



If **50 MW** beam power considered as a limit $\rightarrow I_e = 68\text{mA}$ $N_e = 1.3 \cdot 10^{10}$

$$5000 \text{ h/y} \times 50\text{MW} \times 10 = 250 \text{ GWh/y}$$

Design Task: e-Ring and IR Design which provides

$$\sqrt{\beta_{xp} \cdot \beta_{yp}} = 1m$$

- sufficient dynamic aperture
- With matched beams,
- Small crossing angle $\theta < \sigma_{xe}/\sigma_p$
- Small hour glass effect $\beta_{ye} \geq \sigma_p$
- tolerable synchrotron radiation background
- feasible components

e-Ring Lattice Parameters

bend radius & circumference fixed by LHC effective FODO structure
chosen (no alternative) the only choice to be made is the FODO cell
length or the number of cell length of the arc

→ This determines the lepton beam **emittance** and the **dynamic aperture**

Constraints under the assumption of matched beam sizes at the IP:

Small emittance → large β^* → strong beam-beam effect → no stability
large emittance → small β^* → strong hourglass effect → less lumi
Long cells → large emittance → reduced dynamic aperture → no stability
Short cell → small emittance, high cost

Dynamic Aperture Scaling

$$n_{\sigma}(N, \phi) = \frac{\zeta}{m_{\mathbf{x}}(N, \phi) \cdot \sqrt{\varepsilon(N, \phi) \cdot \beta_f(N, \phi)^3}}$$

Taken
from
HERA:
0.2

for FODO cell structure, N number of FODO Cells

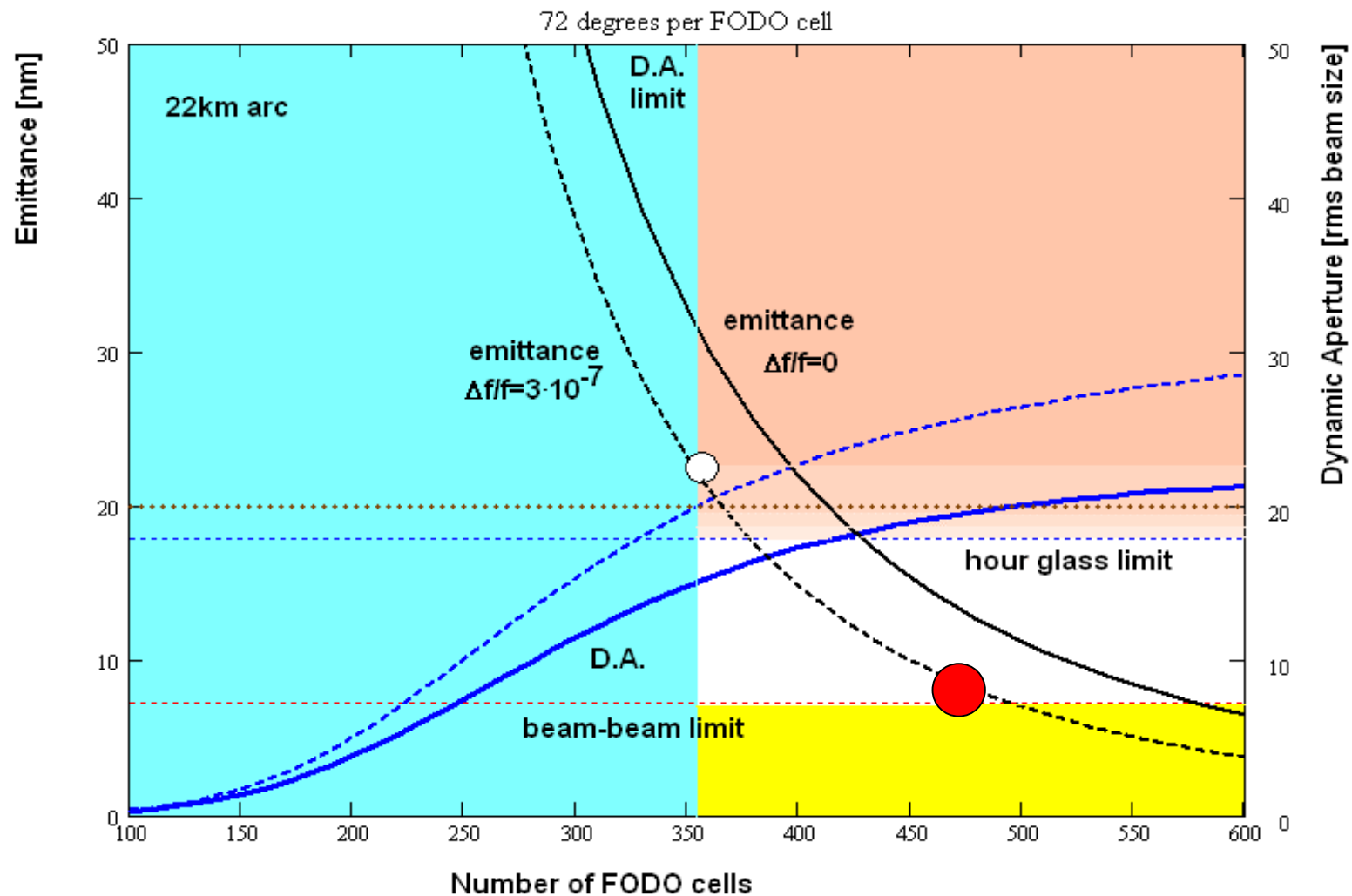
This
assumes a
Plain FODO
structure

$$n_{\sigma}(N, \phi) = \frac{\left(1 + \frac{1}{2} \sin\left(\frac{\phi}{2}\right)\right) \cdot \zeta \cdot \cos\left(\frac{\phi}{2}\right) \cdot \sqrt{2 \sin^2\left(\frac{\phi}{2}\right) - \frac{\pi \cdot (C - L_s)}{N^2 \cdot \rho}}}{\left[\underbrace{\tan\left(\frac{1}{2} \cdot \phi\right)}_{\text{Arc chromaticity}} + \frac{D_{\text{eff}} \cdot \left[C_q \cdot \gamma^2 \cdot \frac{(2\pi)^2 \cdot C - L_s}{2 \cdot N^4 \cdot \rho} \cdot \left(1 - \frac{1}{2} \sin^2\left(\frac{\phi}{2}\right)\right) \right]}{\underbrace{\varepsilon_p \cdot \beta_p \cdot \sin(\phi) \cdot \left[2 \sin^2\left(\frac{\phi}{2}\right) - \frac{\pi \cdot (C - L_s)}{N^2 \cdot \rho} \right]}_{\text{IR chromaticity for matched beams}}} \right] \cdot \sqrt{C_q \cdot \gamma^2 \cdot \frac{8}{\rho} \cdot \left(1 - \frac{1}{2} \sin^2\left(\frac{\phi}{2}\right)\right) \cdot \left(1 + \sin\left(\frac{\phi}{2}\right)\right)^3}}$$

Arc chromaticity

IR chromaticity for matched beams

Choosing Lepton Ring Lattice Parameters



Main Parameters of LeHC

Property	Unit	Leptons	Protons
Beam Energies	GeV	70	7000
Total Beam Current	mA	74	544
Number of Particles / bunch	10^{10}	1.04	17.0
Horizontal Beam Emittance	nm	7.6	0.501
Vertical Beam Emittance	nm	3.8	0.501
Horizontal β -functions at IP	cm	12.7	180
Vertical β -function at the IP	cm	7.1	50
Energy loss per turn	GeV	0.707	$6 \cdot 10^{-6}$
Radiated Energy	MW	50	0.003
Bunch frequency / bunch spacing	MHz / ns	40 / 25	
Center of Mass Energy	GeV	1400	
Luminosity	$10^{33} \text{ cm}^{-2} \text{ s}^{-1}$	1.1	

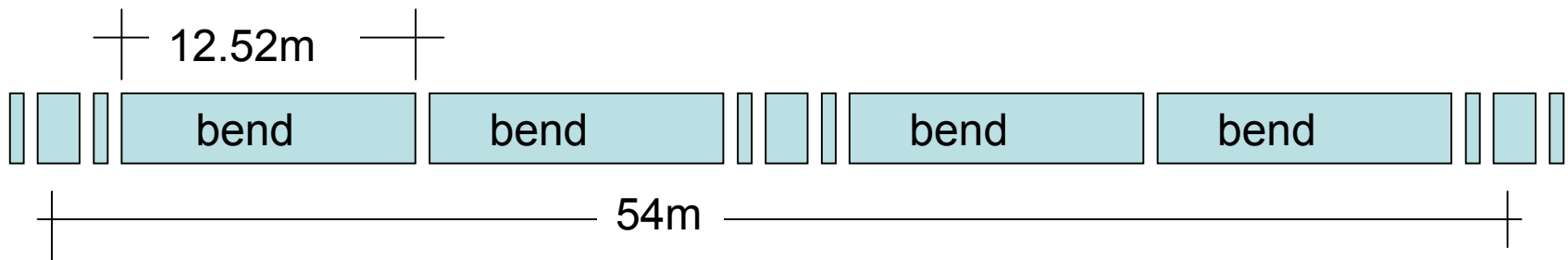
e Lattice

8 Octants with 500m Straight section each

376 FODO cells, Cell length 60.3 m

Dipole length 2×12.52 m $B = 810$ Gauss

Quadrupole length 1.5 m ($G = 8$ T/m)

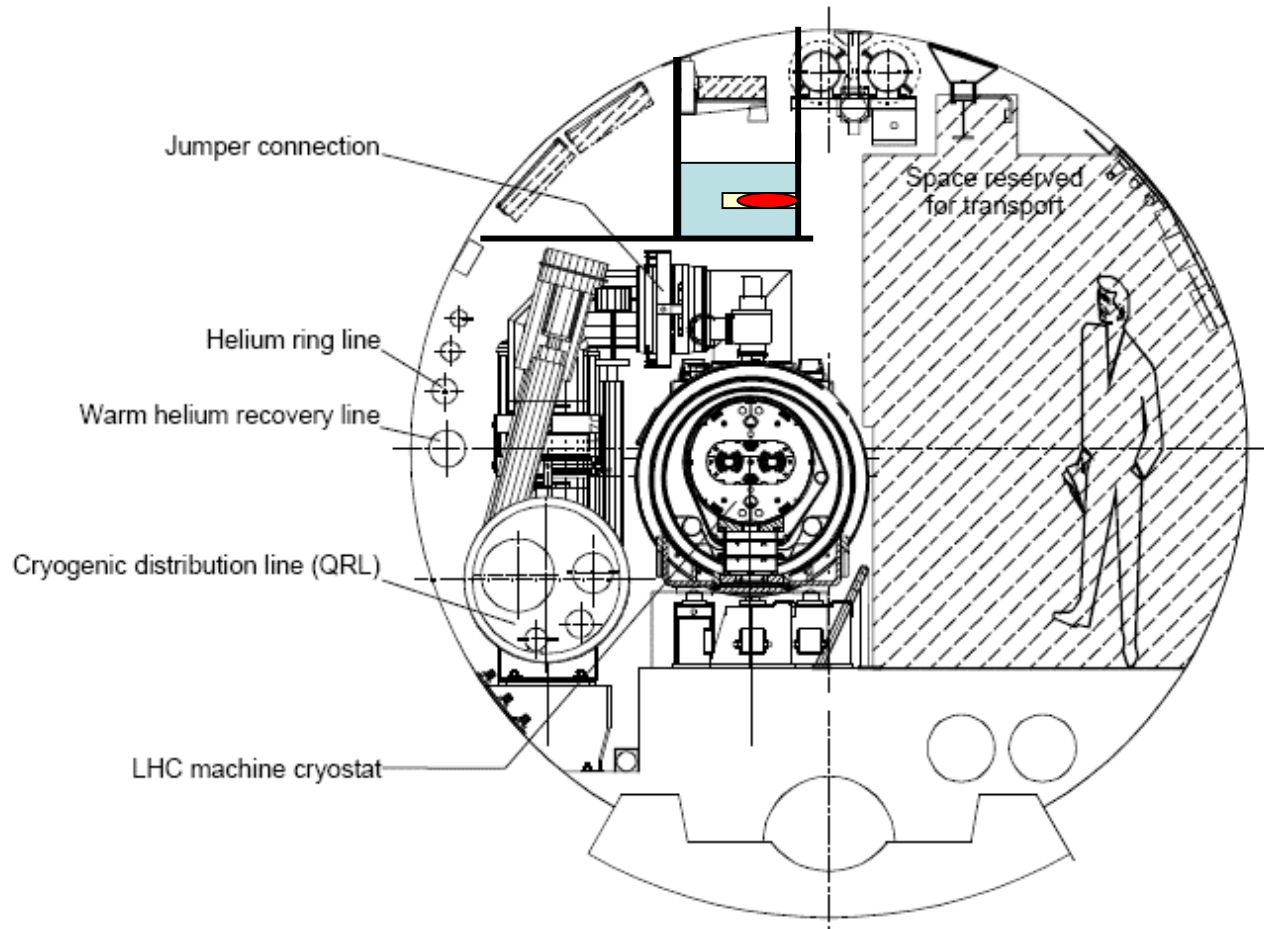


$$\Delta\phi_{\text{fodo}} = 72 \text{ degree}$$

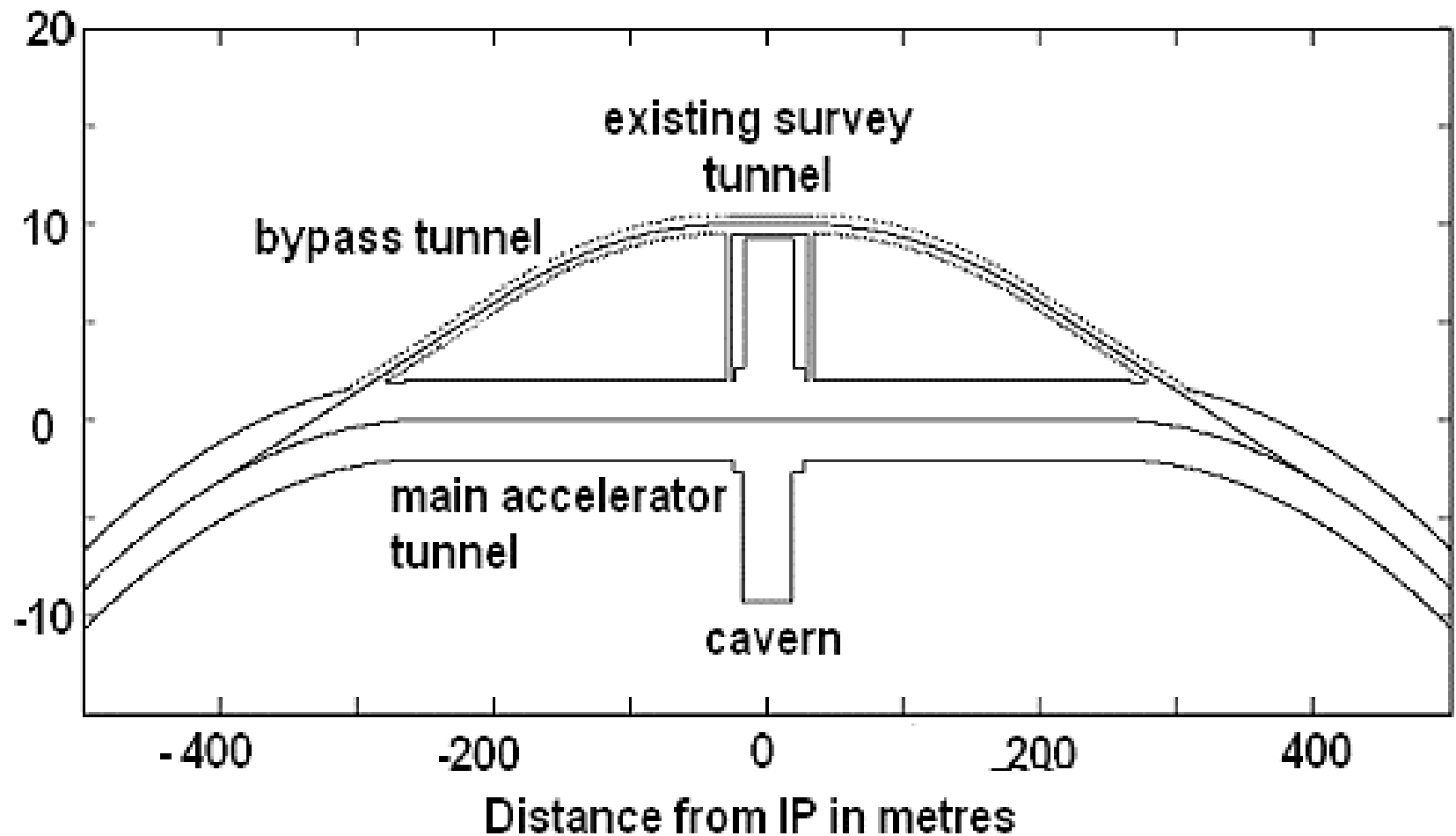
$$\epsilon_{xe} = 8 \text{ nm}$$

Electron Ring Parameters		
Parameter	Unit	Value
Circumference C	m	26658.86
Beam Energy E_e	GeV	70
Arc Focusing		FODO
Cell length L_c	m	60.3
Bending radius ρ	m	2997
Horizontal betatron Phase Adv./cell $\Delta\phi_x$	degree	72
Vertical betatron Phase Adv./cell $\Delta\phi_y$	degree	72
Number of FODO cells in the Arcs N_{cell}		376
Arc Chromaticity (hor/vert.) $\xi_{x,y}$		94/120
Beam Current I_e	mA	70.7
Bunch spacing τ_b	ns	25
Number of bunches n_b		2800
Number of particles per bunch N_e	10^{10}	1.4
Momentum compaction factor α	10^{-4}	1.34
Horizontal beam emittance ϵ_{x0}	nm	7.6
Vertical beam emittance ϵ_{y0}	nm	3.8
RMS energy spread σ_e	10^{-3}	2.4
RMS bunch length	mm	7.1
Particle Radiation energy loss per turn eU_{loss}	MeV/turn	706.8
Beam Power loss P_{loss}	MW	50
Circumferential Voltage U	MV	1521
Synchronous Phase ϕ_{synch}	degree	27
RF frequency f_{rf}	MHz	1000
Bucket height h_b	σ_e	8.4
RF frequency shift	Hz	250
Synchrotron frequency f_s	f_{rev}	0.191

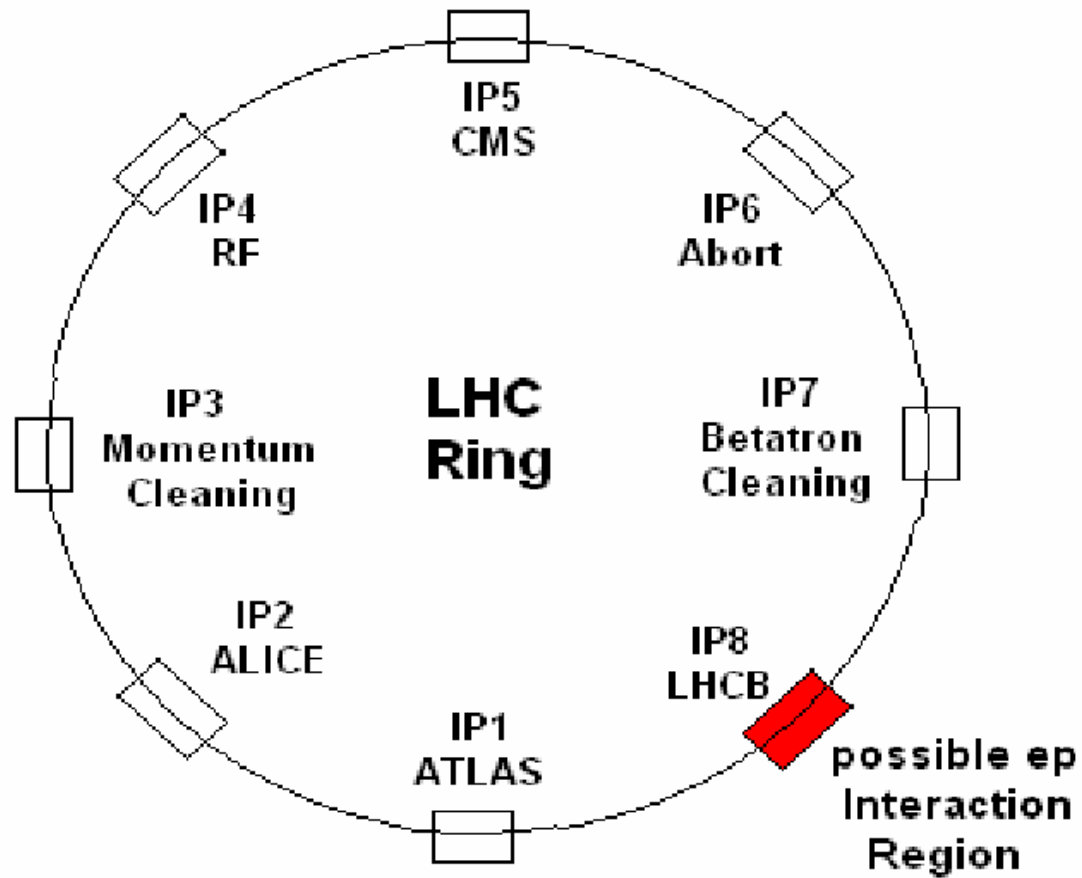
Tunnel Cross Section



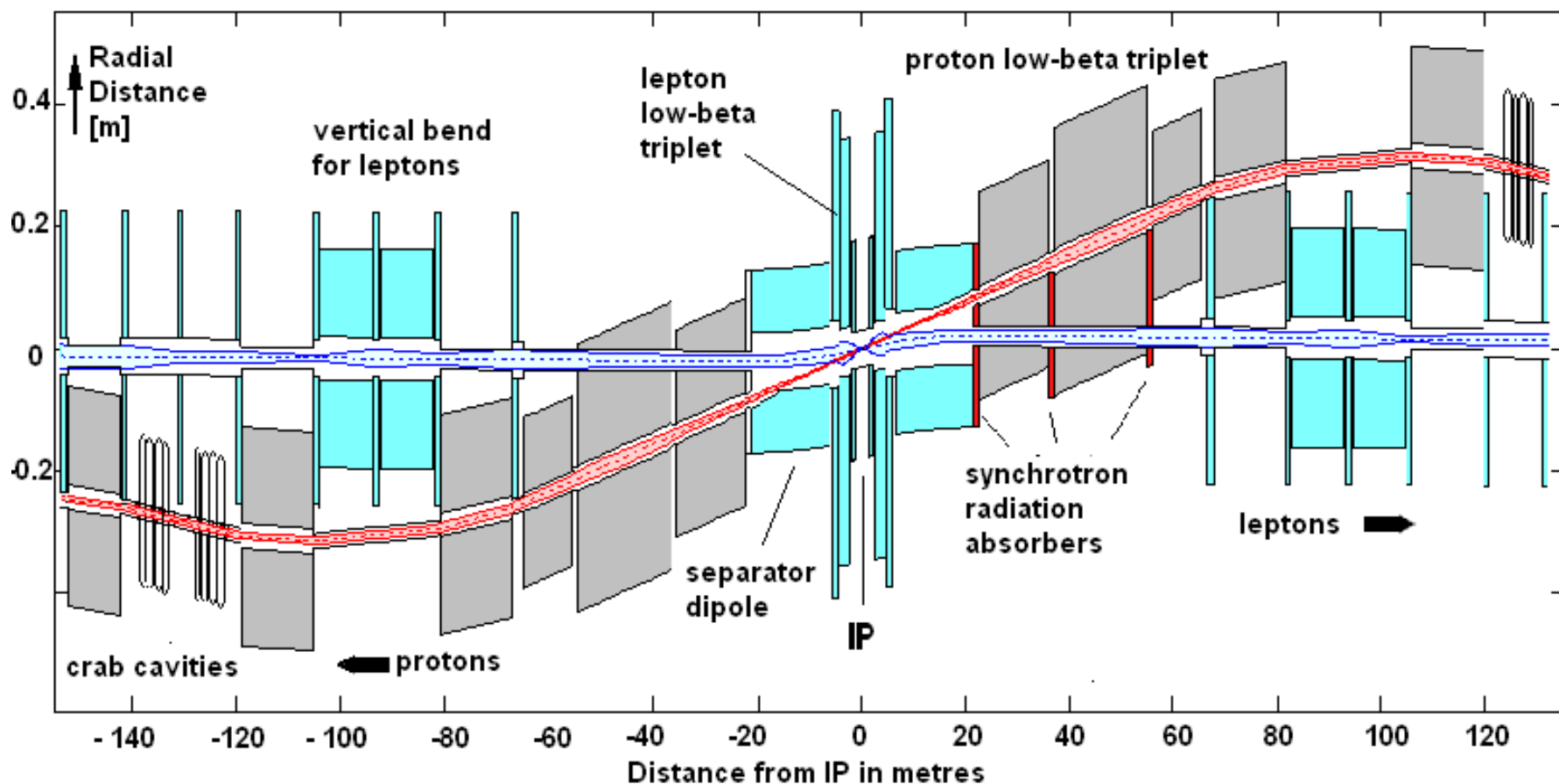
Bypass around Atlas and CMS



Which IR?



IR Layout



Interaction region parameters			
property	unit	leptons	protons
Horizontal Beta function at IP	cm	12.7	180
Vertical beta function at IP	cm	7.07	50
Horizontal IR Chromaticity		-7.5	-7.9
Vertical IR chromaticity		-29.7	-7.7
Maximum horizontal Beta	m	131.7	2279
Maximum vertical Beta	m	704.4	2161
Minimum of available Aperture	σ_x	16	13.5
Low beta quadrupole gradient	T/m	93.3	115
Separation dipole field	T	0.033	-
Synchrotron Radiation Power	kW	9.1	-
Low beta quadrupole length	m	.96/2.43/1.14	16.5/18.6/11
Low beta quadrupole apertures	mm	30/40/50	12/15/15
Distance of first quadruple from IP	m	1.2	22
Detector Acceptance Polar Angle	degree	9.4	
Crossing Angle	mrad	2	

IR Parameters

$$\sigma_{xp} = \sigma_{xe}, \quad \sigma_{yp} = \sigma_{ye}$$

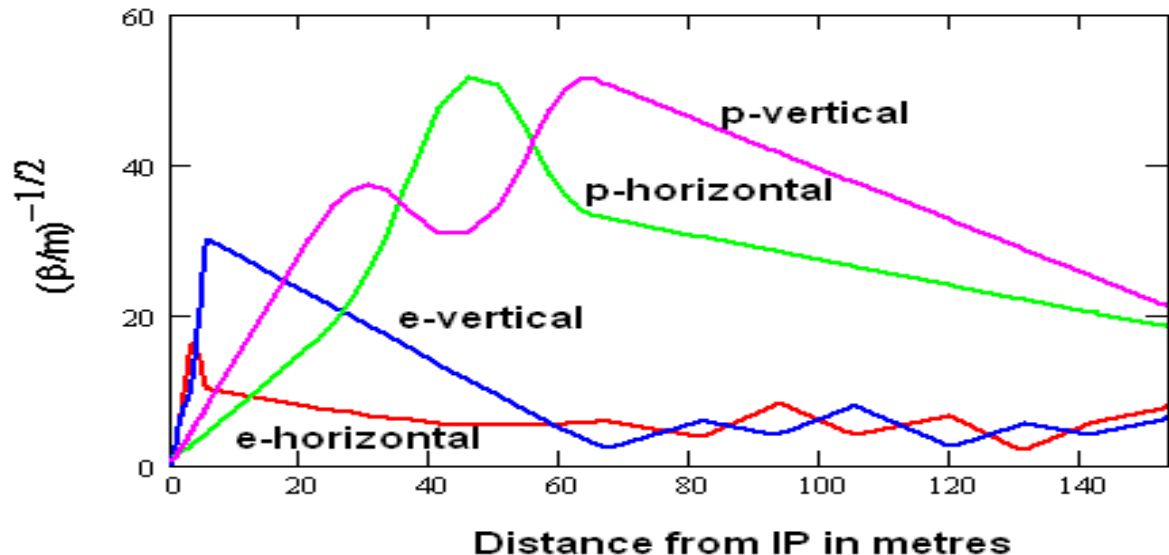
$$\varepsilon_{xp} = 0.5 \text{ nm} \quad \varepsilon_{xe} = 7.6 \text{ nm}$$

Need to match “flat” e beam with “round” p beam

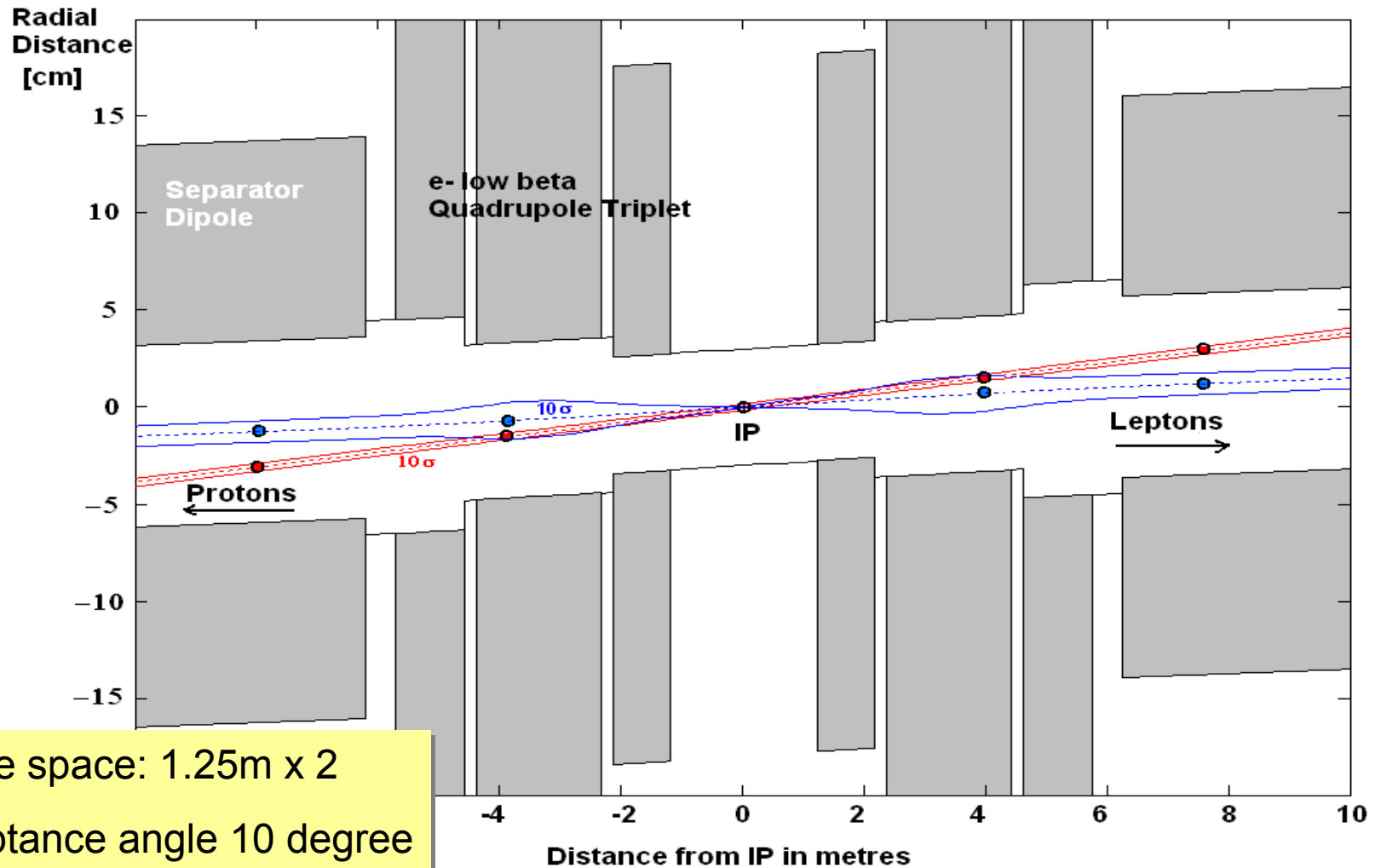
$$\beta_{xp}/\beta_{yp} \approx 4$$

IR optics with low-beta triplets for both e and p beams

$$\begin{aligned} \beta_{xp} &= 1.8 \text{ m} \\ \beta_{yp} &= 0.5 \text{ m} \\ \beta_{xe} &= 12.7 \text{ cm} \\ \beta_{ye} &= 7.1 \text{ cm} \end{aligned}$$



IR Layout



IR free space: 1.25m x 2

Acceptance angle 10 degree

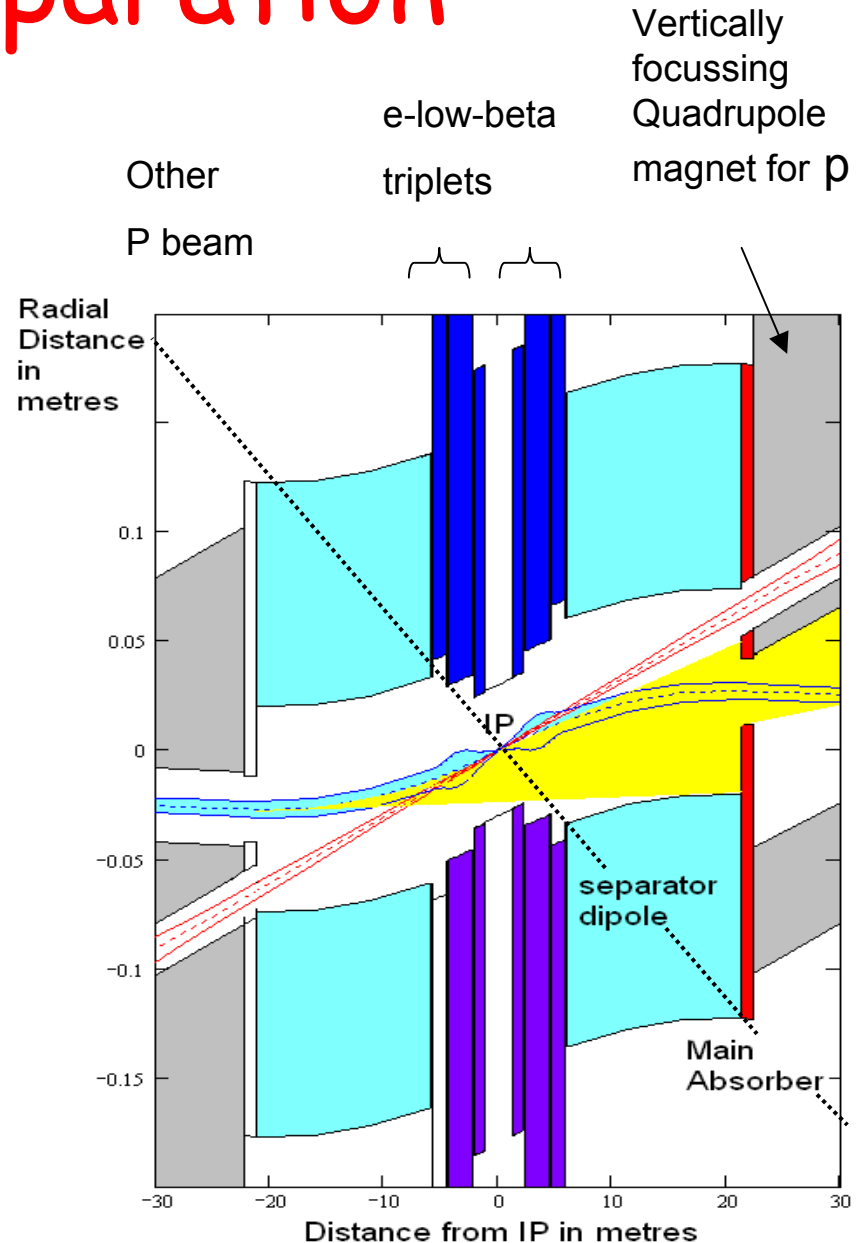
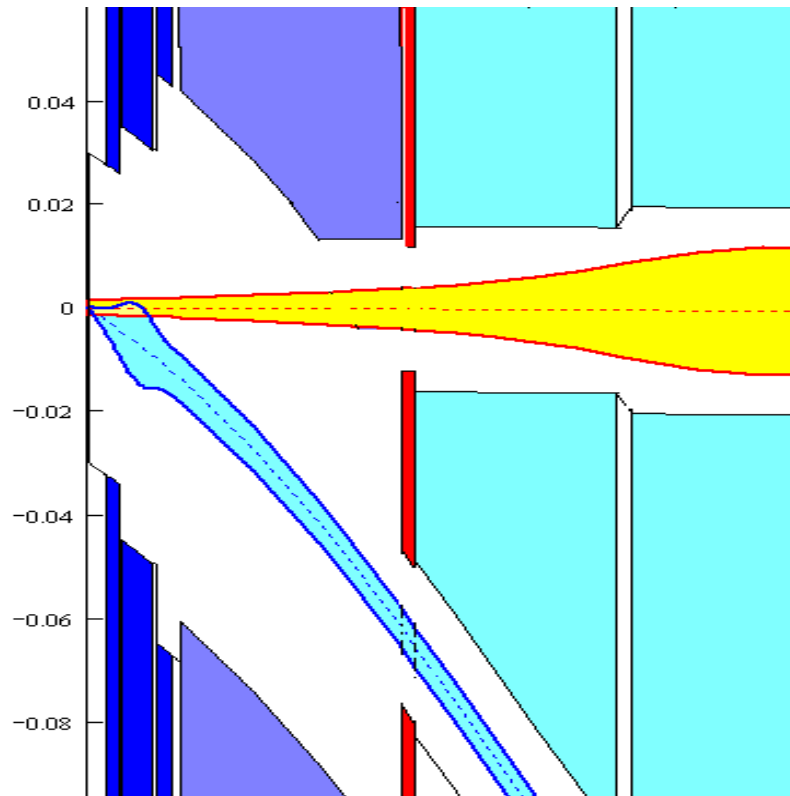
Crossing angle 2mr

Beam Separation

Crossing angle 2mr

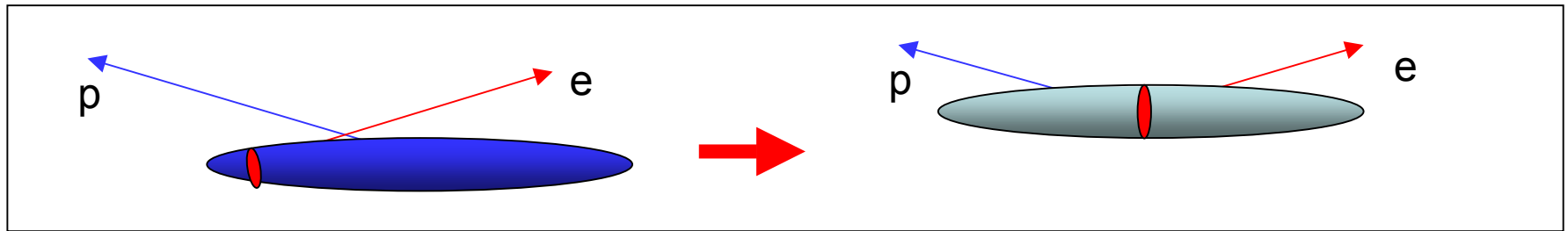
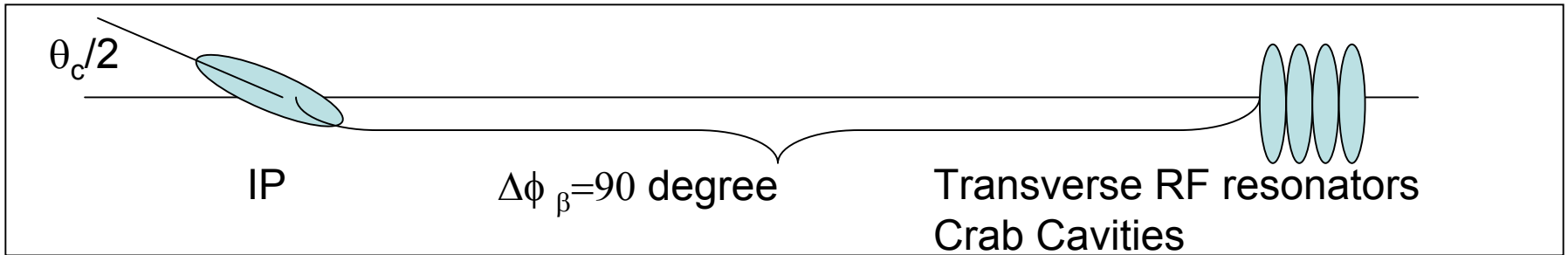
Magnetic separation 2mr

→ 60 mm separation @20m

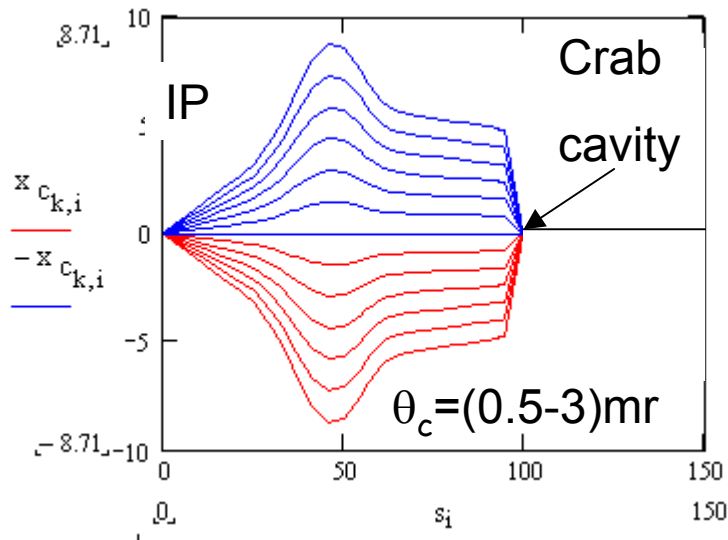


Crab Crossing

Crossing angle will enhance effective beam size $\sigma^2 = \varepsilon\beta + \theta^2\sigma_s^2$



“Crabbed Trajectories”



Crab Cavity Calculations

Required Crossing Angle $k_s := 42$

ep Separation $x_{p_{k_s}} - x_{e_{k_s}} = 65.571 \text{ mm}$ $s_{k_s} = 22.232 \text{ m}$

$\Delta x_{\text{sep}} := x_{p_{k_s}} - x_{e_{k_s}}$ $\theta_r := \theta_c$ $\theta_r = -2 \text{ mrad}$

required crab cavity orbit kick for $1\sigma \Delta\sigma/\sigma$ particles

$x_r := \frac{\theta_r}{2} \cdot \sigma_s$ $\beta_{px_0} = 1.8 \text{ m}$ $\beta_{px_{82}} = 708.766 \text{ m}$

$\theta_{cc} := \frac{-x_r}{\sqrt{\beta_{px_0} \cdot \beta_{px_{82}}}}$ $\theta_{cc} = 2.1 \mu\text{rad}$

crab cavity frequency $f_{cc} := 0.5 \cdot \text{GHz}$

$\lambda_{cc} := \frac{c}{f_{cc}}$ $\lambda_{cc} = 599.585 \text{ mm}$ $\sigma_s = 75 \text{ mm}$

crab cavity phase of one sigma particle $\phi_{cc1s} := \frac{2 \cdot \pi \cdot \sigma_s}{\lambda_{cc}}$ $\phi_{cc1s} \cdot \frac{180}{\pi} = 45.031$

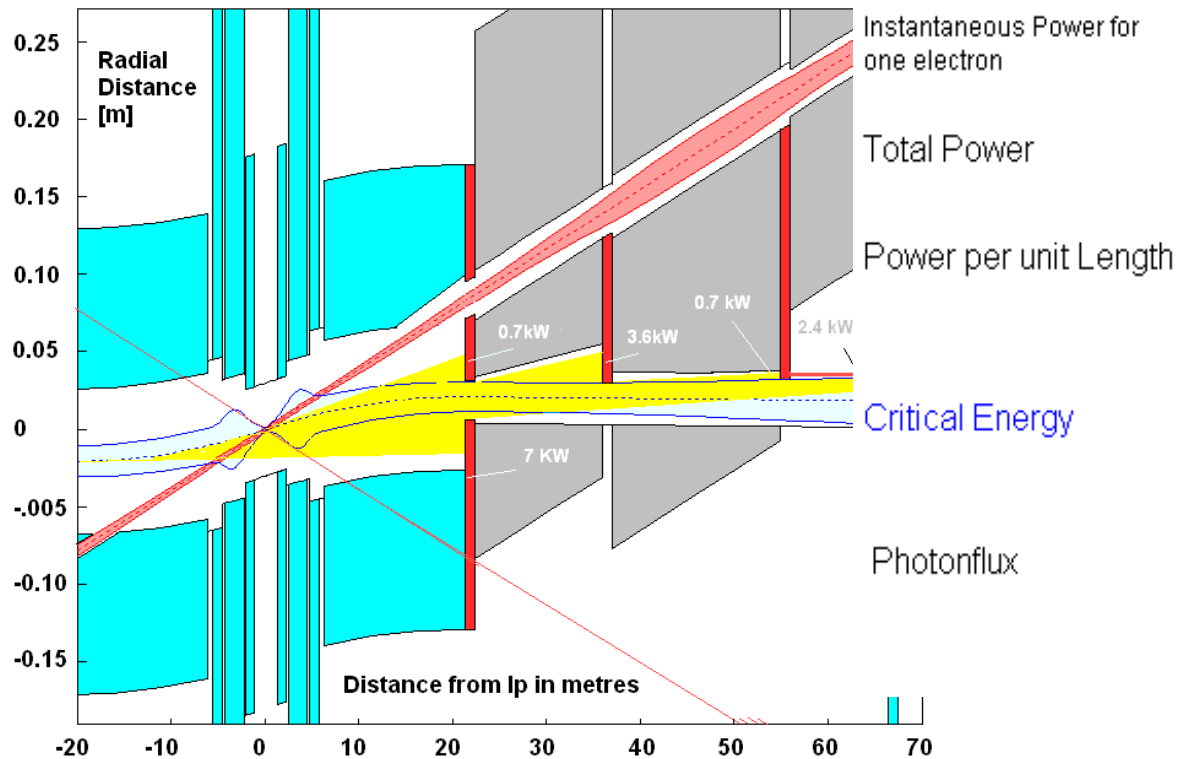
Required cavity voltage: $U_{cc} := \frac{\theta_{cc} \cdot E_p}{e \cdot \sin(\phi_{cc1s})}$ $U_{cc} = 20.775 \text{ MV}$

achievable gradient: $G_{cc} := 3.4 \cdot \text{MV} \cdot \text{m}^{-1}$

Length of the cc structure: $L_{cc} := \frac{U_{cc}}{G_{cc}}$ $L_{cc} = 6.11 \text{ m}$

Synchrotron Radiation

$$\rho_{ir} = 10000 \text{ m}$$



$$P_g(E_e, \rho_{ir}) = 1.615 \times 10^{-7} \text{ watt}$$

$$2 \cdot P_{\text{syn}}(E_e, \rho_{ir}, \theta_{ir}, I_e) = -9.111 \text{ kW}$$

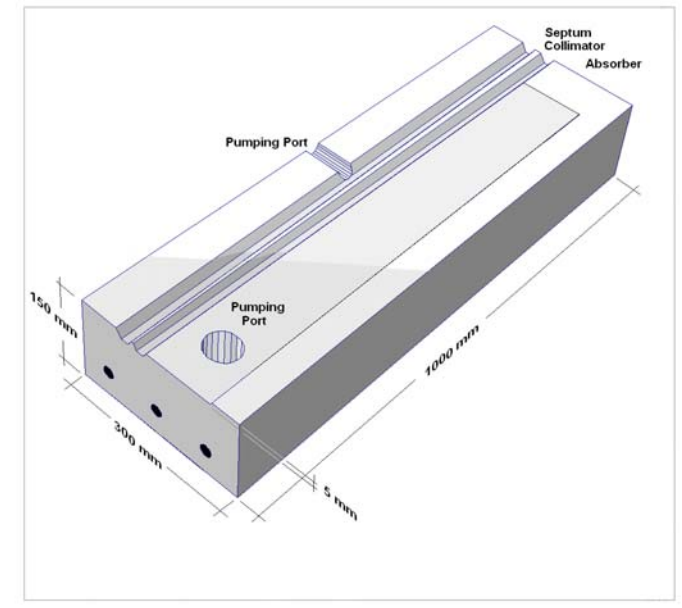
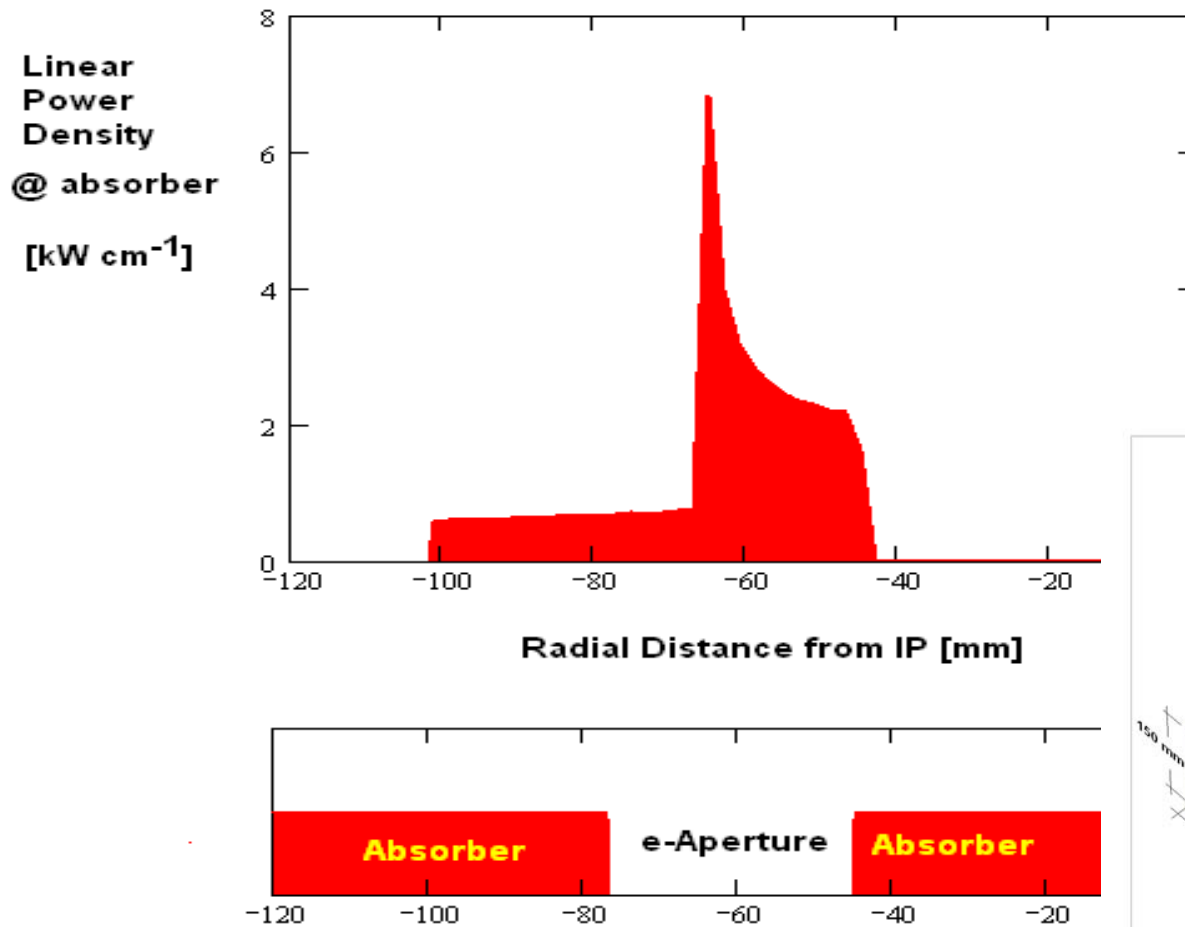
$$P_s(E_e, \rho_{ir}, I_e) = 0.238 \text{ kW} \cdot \text{m}^{-1}$$

$$u_c(E_e, \rho_{ir}) = 76.137 \text{ keV}$$

$$\Phi_{\text{ph}}(E_e, \rho_{ir}, I) = 2.957 \times 10^{19} \frac{1}{\text{msA}}$$

$$\rho_{ir} = -1.001 \times 10^4 \text{ m} \quad L_{ir} = 19.132 \text{ m}$$

SR Power Density on Absorber



ep Collision Parameters and Luminosity

E	$E_p = 7 \times 10^3 \text{ GeV}$	$E_e = 70 \text{ GeV}$		
I	$I_p = 0.856 \text{ A}$	$I_e = 0.071 \text{ A}$		
N	$N_p = 1.7 \times 10^{11}$	$N_e = 1.404 \times 10^{10}$		
β^*	$\beta_{xp} = 180 \text{ cm}$	$\beta_{xe} = 12.73 \text{ cm}$	$\max(\beta_{py}) = 2.637 \times 10^3 \text{ m}$	$\max(\beta_{ey}) = 704.454 \text{ m}$
	$\beta_{yp} = 50 \text{ cm}$	$\beta_{ye} = 7.072 \text{ cm}$	$\max(\beta_{px}) = 2.668 \times 10^3 \text{ m}$	$\max(\beta_{ex}) = 131.728 \text{ m}$
Beam size	$\sigma_{xp} = 31.066 \mu\text{m}$	$\sigma_{xe} = 31.066 \mu\text{m}$		
	$\sigma_{yp} = 16.373 \mu\text{m}$	$\sigma_{ye} = 16.373 \mu\text{m}$		
	$\sigma_s = 75 \text{ mm}$	$\sigma_{be} = 7.085 \text{ mm}$		
IR Chromaticity	$\xi_{pxIR} = -7.969$	$\xi_{exIR} = -7.517$		
	$\xi_{pyIR} = -7.74$	$\xi_{eyIR} = -29.757$		
beam-Beam Tuneshift	$\Delta v_{xp} = 8.318 \times 10^{-4}$	$\Delta v_{xe} = 0.048$	$\Delta v_{xpar} = 0.029 \cdot 10^{-3}$	
	$\Delta v_{yp} = 3.177 \times 10^{-4}$	$\Delta v_{ye} = 0.051$	$\Delta v_{ypar} = -0.444 \cdot 10^{-3}$	
Crossing Angle	$\theta_c = -2 \text{ mr}$			
Hourglass factor	$R(\sigma_s) = 0.947$			
Peak Luminosity	$L_{\text{peak}} = 1.103 \times 10^{33} \text{ sec}^{-1} \cdot \text{cm}^{-2}$			

Beam-Beam Effect

Central crossing beam-beam parameters well within the HERA range

e-hor bb tuneshift

$$\Delta\nu_{xe} := \frac{r_e \cdot N_p \cdot \beta_{xe}}{2 \cdot \pi \cdot \gamma_e \cdot \sigma_{xp} \cdot (\sigma_{xp} + \sigma_{yp})} \quad \Delta\nu_{xe} = 0.048$$

e ver bb tuneshift

$$\Delta\nu_{ye} := \frac{r_e \cdot N_p \cdot \beta_{ye}}{2 \cdot \pi \cdot \gamma_e \cdot \sigma_{yp} \cdot (\sigma_{xp} + \sigma_{yp})} \quad \Delta\nu_{ye} = 0.051$$

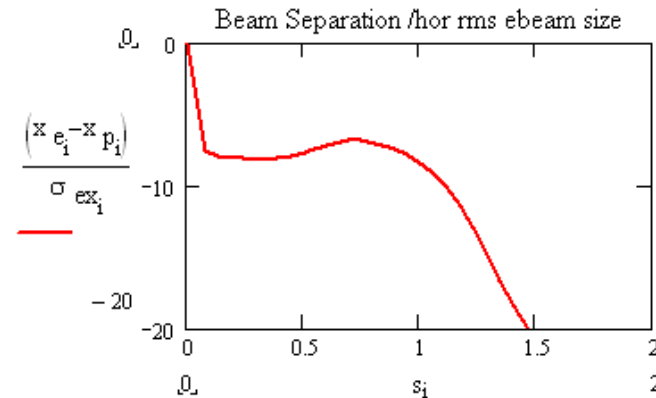
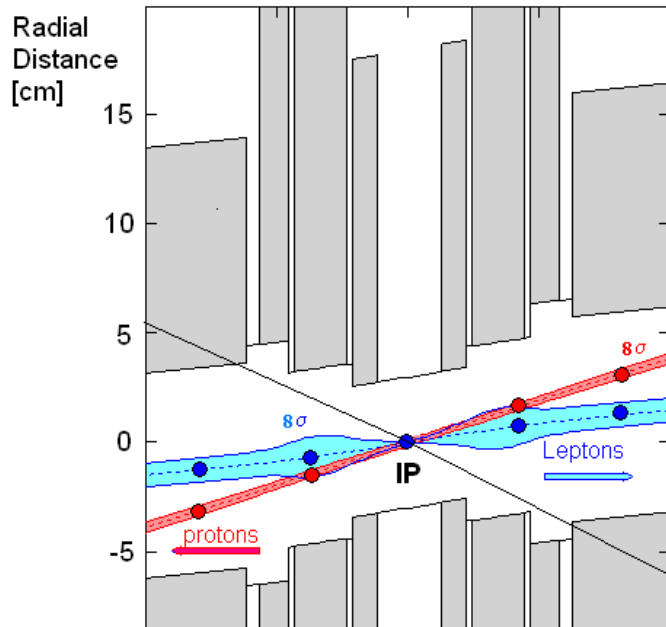
p-hor bb tuneshift

$$\Delta\nu_{xp} := \frac{r_p \cdot N_e \cdot \beta_{xp}}{2 \cdot \pi \cdot \gamma_p \cdot \sigma_{xe} \cdot (\sigma_{xe} + \sigma_{ye})} \quad \Delta\nu_{xp} = 5.122 \times 10^{-4}$$

p ver bb tuneshift

$$\Delta\nu_{yp} := \frac{r_p \cdot N_e \cdot \beta_{yp}}{2 \cdot \pi \cdot \gamma_p \cdot \sigma_{ye} \cdot (\sigma_{xe} + \sigma_{ye})} \quad \Delta\nu_{yp} = 2.7 \times 10^{-4}$$

Parasitic Crossings



$$\Delta v_x^{\text{par}} = \frac{N_p r_0 \beta_x^{\text{par}}}{2\pi \gamma_e \Delta x^3}$$

$$\Delta v_y^{\text{par}} = \frac{-N_p r_0 \beta_y^{\text{par}}}{2\pi \gamma_e \Delta x^3}$$

Bunch spacing	Crossing angle	Separation	Separation	Horizont. parasitic beam-beam tune shift	Vertical parasitic beam-beam tune shift
[ns]	[mrad]	[mm]	$[\sigma_x]$		
25	2.0	7.7	8.3	0.0011	-0.0015
50	2.0	15	23	0.0001	-0.002
75	2.0	27	50	0.00003	-0.0004

Luminosity vs Bunch Spacing

L independent of bunch spacing

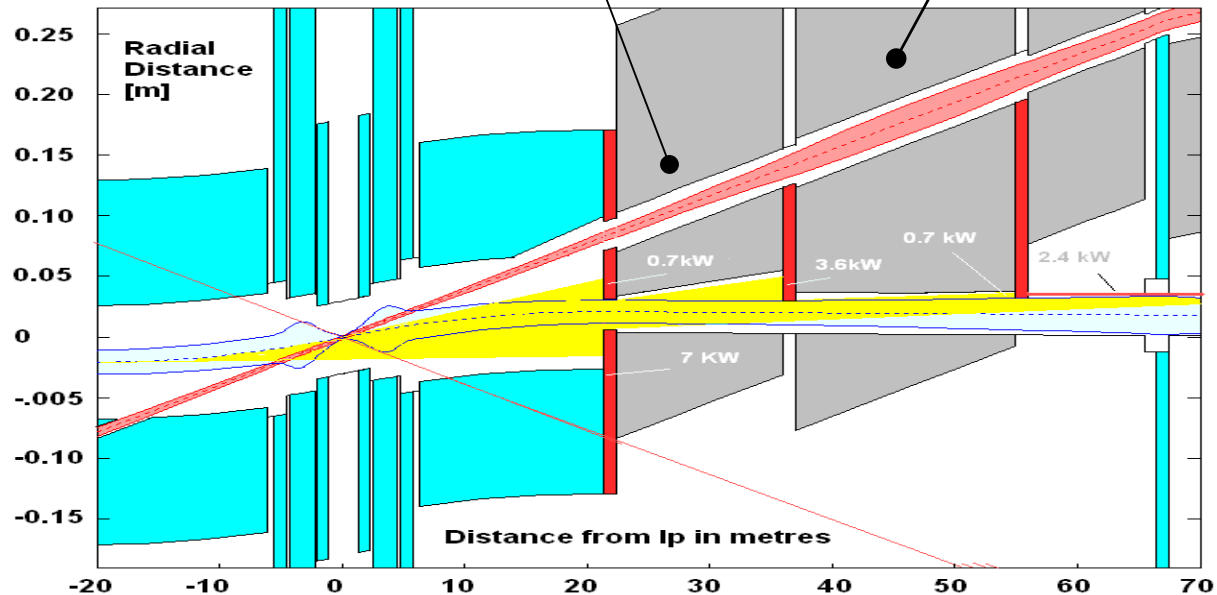
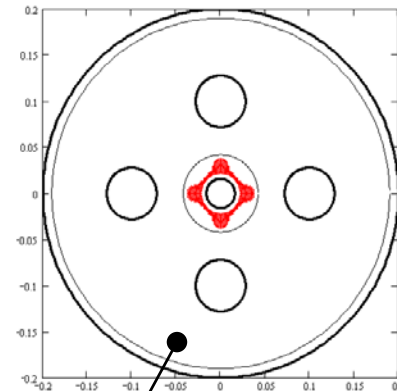
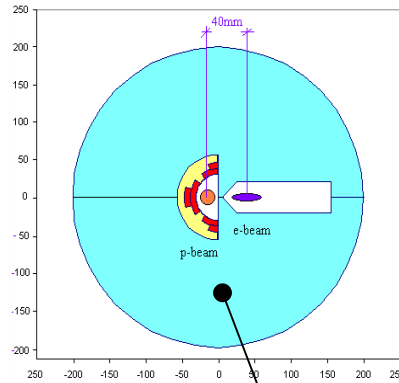
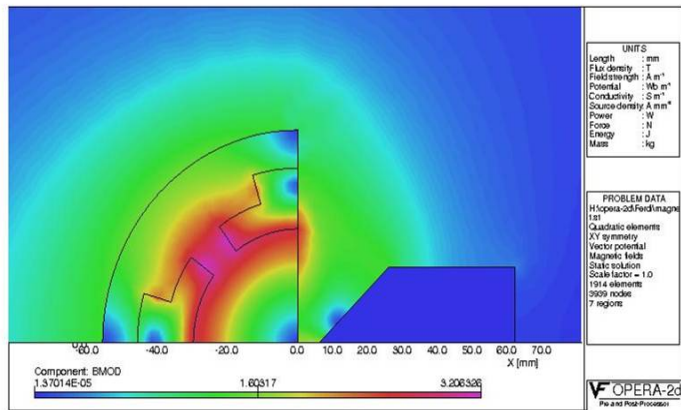
As long as I_e total can be maintained

At very large bunch spacings limitations by
Proton beam-beam effect

Single bunch instabilities of e-beam

up to 75ns bunch spacing far from
becoming a problem

Quadrupole Magnets



Conclusions

A first look at a possible lepton proton collider in the LHC tunnel with a luminosity of $10^{33}\text{cm}^{-2}\text{s}^{-1}$ appears to be technical possible

Simultaneous operation of pp and ep should be possible (however with reduced pp luminosity)

More work is needed to determine the most optimum parameters, the optimum technical choices and the cost of such a facility

A workshop to discuss this exciting option together with experimental physicists and accelerator scientists is envisioned

Further activities on the layout of the accelerator should be coordinated with and integrated into the discussions on LHC upgrades